

ALPs at Colliders

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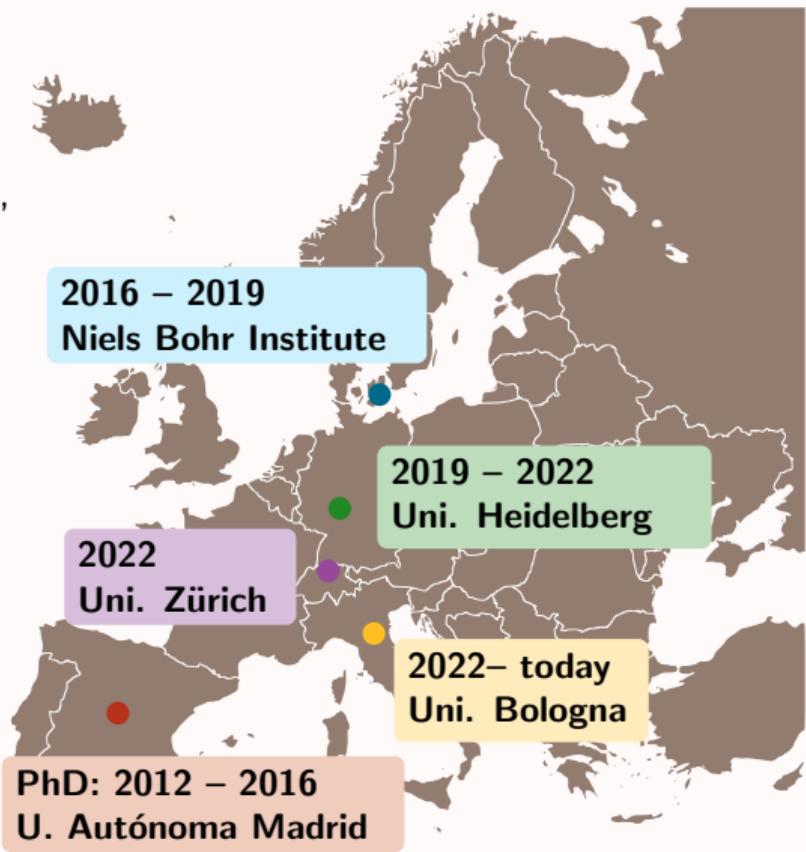
Career Recap

- ▶ research red thread: **Effective Field Theories for BSM**, mostly @LHC

SMEFT, HEFT, ALPs...

- ▶ theory, but close contact with ATLAS/CMS exp

LHC EFT Working Group [2020-2024]
VBSCan COST Action [2018-2021]
COMETA COST Action [2023-2027]



Axion-Like Particles

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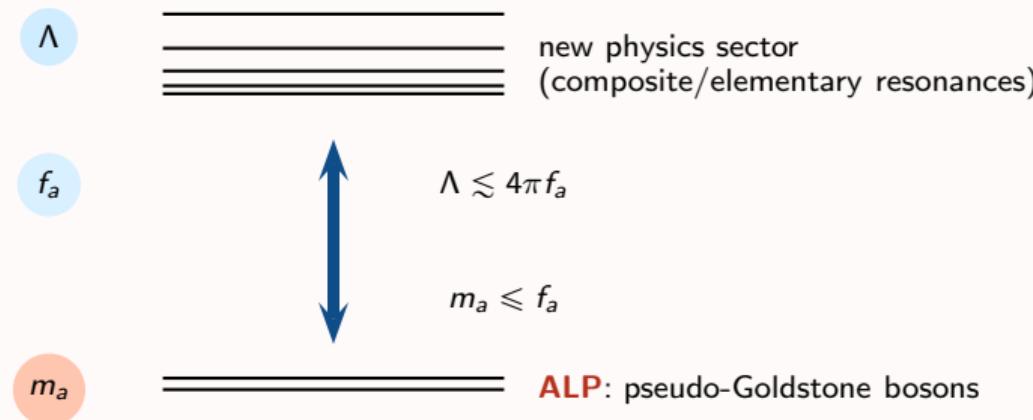
ALP = generic pseudo-Goldstone boson from breaking of BSM symmetry

Examples:

Peccei-Quinn symm. → QCD axion Peccei, Quinn 1977, Weinberg 1978, Wilczek 1978

Lepton number → Majoron Gelmini, Roncadelli 1981, Langacker, Peccei, Yanagida 1986

Flavor symm. → Flavon Wilczek 1982



Axion-Like Particles

ALP = generic pseudo-Goldstone boson from breaking of BSM symmetry

Examples:

Peccei-Quinn symm.	→	QCD axion	Peccei, Quinn 1977, Weinberg 1978, Wilczek 1978
Lepton number	→	Majoron	Gelmini, Roncadelli 1981, Langacker, Peccei, Yanagida 1986
Flavor symm.	→	Flavon	Wilczek 1982

Fundamental properties

- ▶ neutral, pseudo-scalar, couples to SM via effective interactions
- ▶ pseudo-Goldstone boson → **m_a naturally small** compared to NP scale

Why so interesting?

- ▶ naturally the lightest remnant of heavy NP sectors → easiest to discover
- ▶ spontaneous symmetry breakings are **ubiquitous** in BSM → predicted in many models
- ▶ under certain conditions: good **DM** candidate

Original case study: QCD axion

strong CP problem

$$\mathcal{L}_{SM} \supset \bar{\theta} \frac{g_s^2}{32\pi^2} G_{\mu\nu}^A \tilde{G}^{\mu\nu A} \rightarrow \text{CP} \text{ in QCD} \quad \text{neutron EDM requires } \bar{\theta} \lesssim 10^{-10}$$

why so small?

“EFT” Axion solution

promote $\bar{\theta}$ to a dynamical field $\rightarrow a(x)$ neutral pseudo-scalar, f_a scale to suppress dim-5 interaction

$$\mathcal{L} = \frac{1}{2} \partial_\mu a \partial^\mu a + \frac{a}{f_a} \frac{g_s^2}{32\pi^2} G_{\mu\nu}^A \tilde{G}^{\mu\nu A} + \dots$$

trick: proved that it must be $\langle a \rangle = 0 \Rightarrow$ no CP, but a new light DOF coupling to $G \tilde{G}$

UV origin: pseudo-Goldstone boson of Peccei-Quinn symmetry breaking

global, anomalous $U(1)_{PQ}$ defined such that $\partial_\mu J_{PQ}^\mu = \frac{g_s^2}{16\pi^2} N G_{\mu\nu}^A \tilde{G}^{\mu\nu A} + \dots$

broken spontaneously \rightarrow the resulting pGB satisfies the axion properties

The axion Lagrangian

- ▶ neutral pseudo-scalar
- ▶ **approx. shift symmetry** $a(x) \mapsto a(x) + c$ broken by the PQ anomaly ($aG\tilde{G}$ coupling)
- ▶ couples to SM via an **Effective Lagrangian** ($\text{dim} \geq 5$)
- ▶ mass and self-interactions generated non-perturbatively via shift symmetry breaking.
naturally small compared to NP sector

$$\mathcal{L}_a = \frac{1}{2}\partial_\mu a\partial^\mu a + \frac{a}{f_a} \frac{g_s^2}{32\pi^2} G_{\mu\nu}^A \tilde{G}^{\mu\nu A} + \frac{a}{f_a} \frac{e^2}{32\pi^2} \frac{E}{N} F_{\mu\nu} \tilde{F}^{\mu\nu} - \frac{\partial_\mu a}{2f_a} \bar{\psi} C_\psi \gamma^\mu \gamma_5 \psi$$



$$m_a^2 = \frac{m_u m_d}{(m_u + m_d)^2} \frac{m_\pi^2 f_\pi^2}{f_a^2} \sim \frac{10^{-6} \text{ GeV}^4}{f_a^2}$$

+ axion self-couplings, couplings to nucleons and mesons

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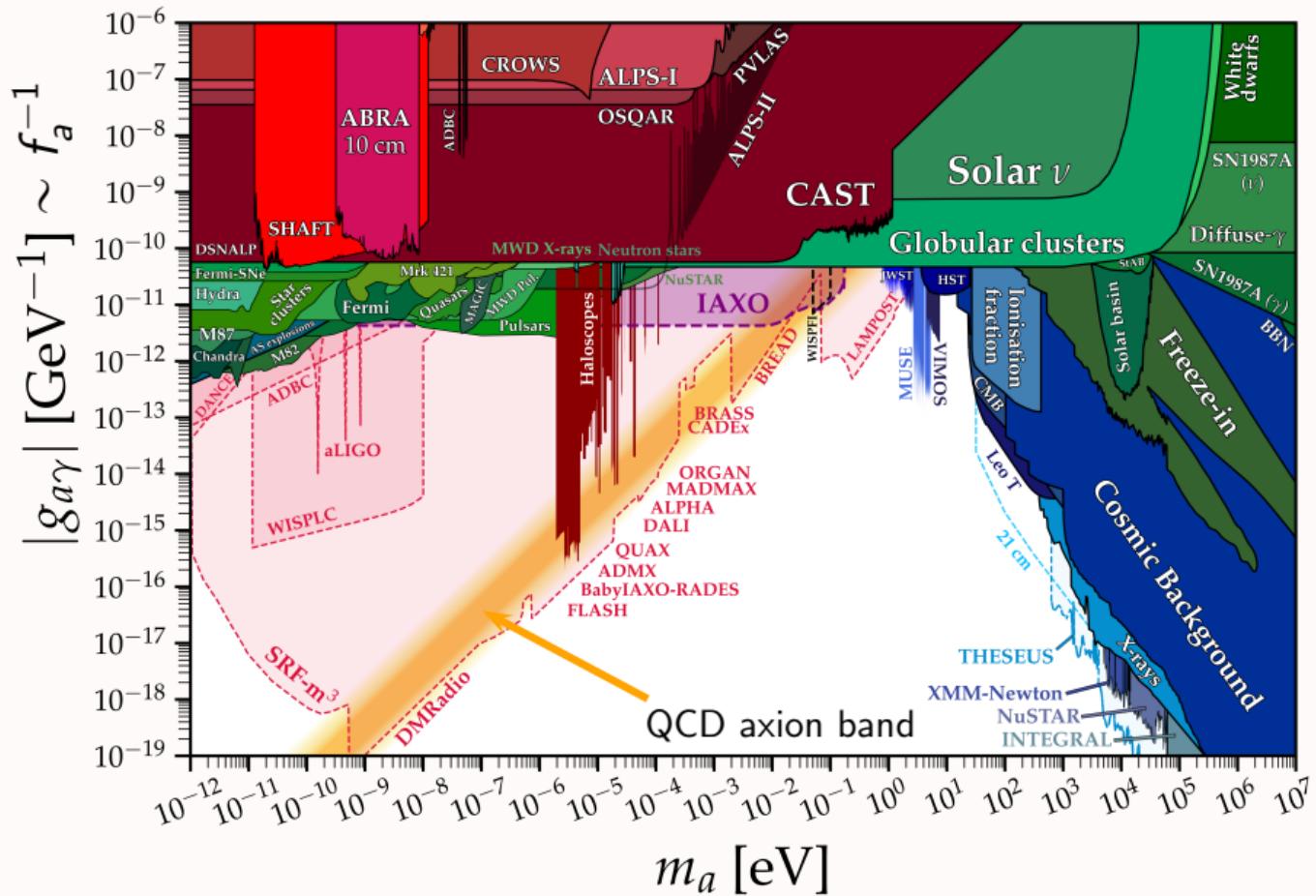


dependent on $U(1)_{PQ}$ realization

$$m_a^2 = \frac{m_u m_d}{(m_u + m_d)^2} \frac{m_\pi^2 f_\pi^2}{f_a^2} \sim \frac{10^{-6} \text{ GeV}^4}{f_a^2}$$

consequence of axion solving strong CP

+ axion self-couplings, couplings to nucleons and mesons



<https://cajohare.github.io/AxionLimits/>

ALP Effective Field Theory

- most general EFT of ALP interactions:
 - $\text{SU}(3) \times \text{SU}(2) \times \text{U}(1)$ invariant (for LHC applications)
 - fields: SM states + ALP
- shift symmetry:** here assume broken only by m_a , but more operators could enter
- assume CP invariance, but CP-odd couplings could be inserted too

review: di Luzio,Levati,Paradisi,Sørensen
2312.17310

$$\mathcal{L}_{ALP} = \frac{1}{2} \partial_\mu a \partial^\mu a - \frac{m_a^2}{2} a^2 + C_i O_i^{(5)} + \mathcal{O}(f_a^{-2})$$

Georgi,Kaplan,Randall PLB169B(1986)73

$$O_{\tilde{B}} = \frac{a}{f_a} B_{\mu\nu} \tilde{B}^{\mu\nu} \quad O_{f,ij} = \frac{\partial^\mu a}{f_a} (\bar{f}_i \gamma^\mu f_j), \quad f = Q_L, u_R, d_R, \ell_L, e_R$$

$$O_{\tilde{W}} = \frac{a}{f_a} W_{\mu\nu}^I \tilde{W}^{I\mu\nu}$$

$$O_{\tilde{G}} = \frac{a}{f_a} G_{\mu\nu}^A \tilde{G}^{A\mu\nu}$$

Parameter space of the ALP EFT at dim-5

Free quantities	$N_f = 1$	$N_f = 3$
m_a	1	1
$C_i/f_a : C_{\tilde{B}}, C_{\tilde{W}}, C_{\tilde{G}} \in \mathbb{R}$	3	3
$C_{f,ij} \in N_f \times N_f$ symmetric \mathbb{R} matrices	5×1	5×6
$-L_i$ rotations	-1	-3
$-(B - L)$ rotation	-1	-1
	7	30

redundancies due to:

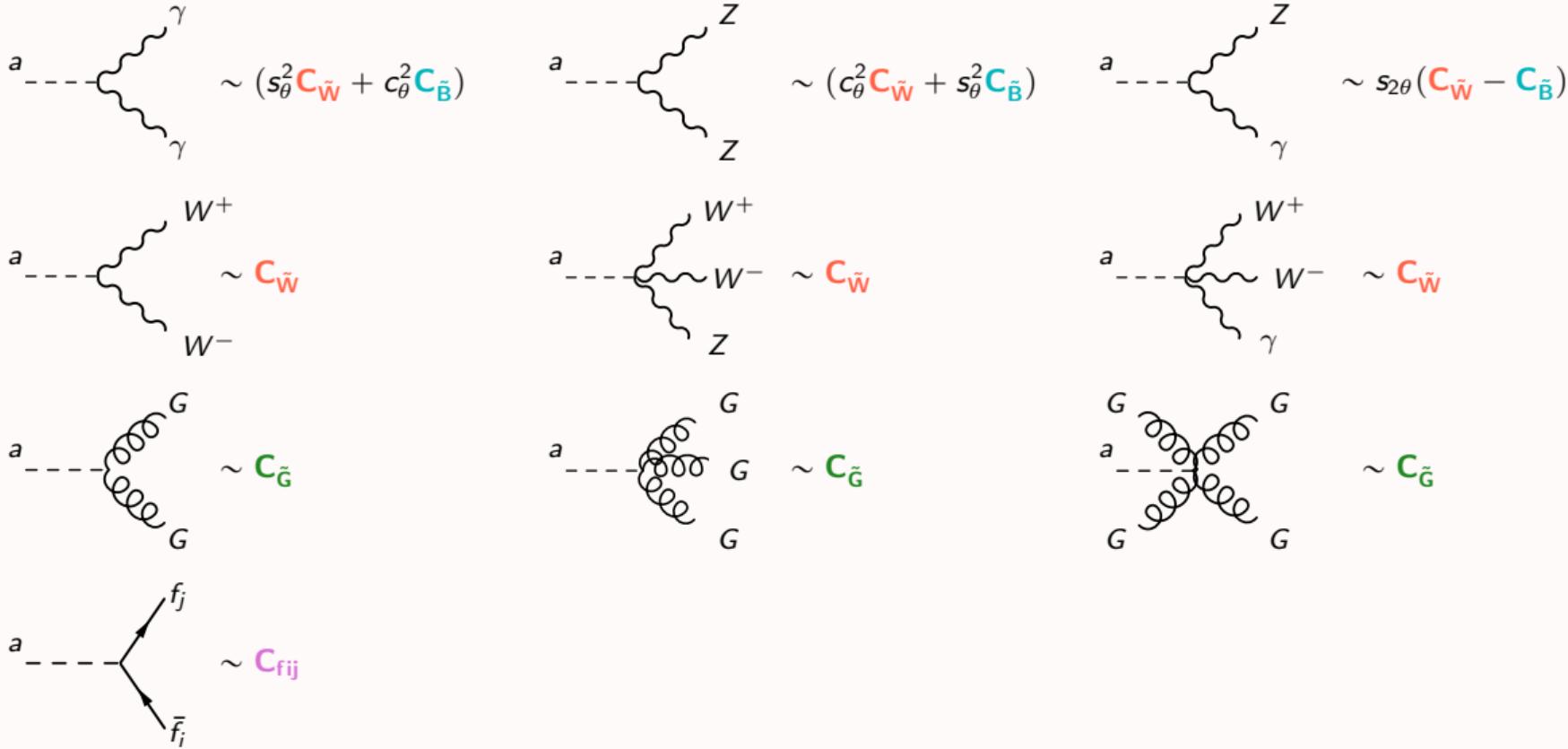
$$\frac{\partial_\mu a}{f_a} J^\mu_{L_i} = O_{\ell,ii} + O_{e,ii} = \frac{1}{32\pi^2} [g^2 O_{\tilde{W}} - g'^2 O_{\tilde{B}}]$$

$$\frac{\partial_\mu a}{f_a} J^\mu_{B-L} = \frac{1}{3} \text{Tr}[O_Q + O_u + O_d] - \text{Tr}[O_\ell + O_e] = 0$$

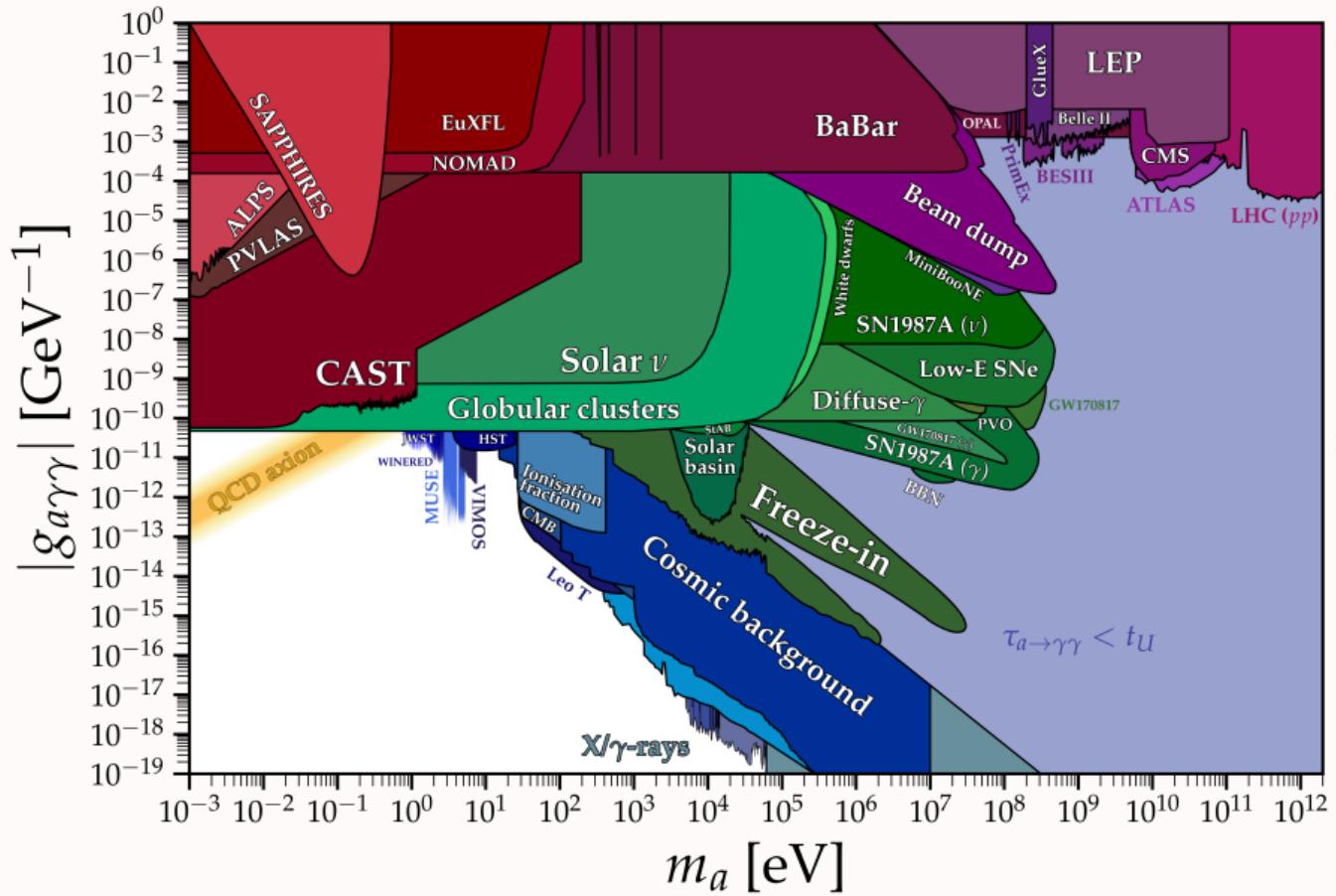
[only visible in 1-loop calculations]

Chala,Guedes,Ramos,Santiago 2012.09017, Bauer,Neubert,Renner,Schnubel,Thamm 2012.12272
 Bonilla,IB,Gavela,Sanz 2107.11392, Bonnefoy,Grojean,Kley 2206.04182

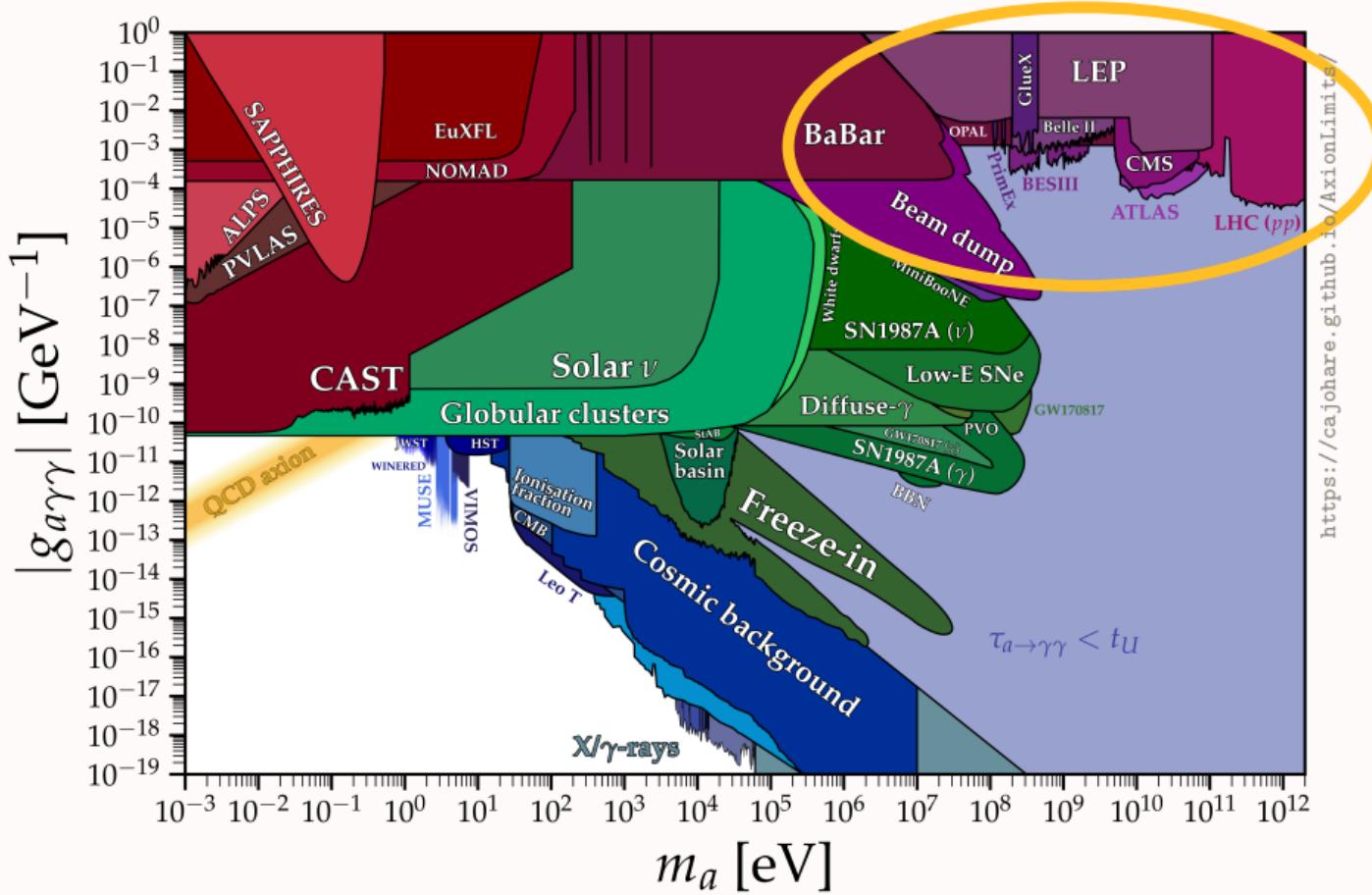
ALP couplings to dim-5



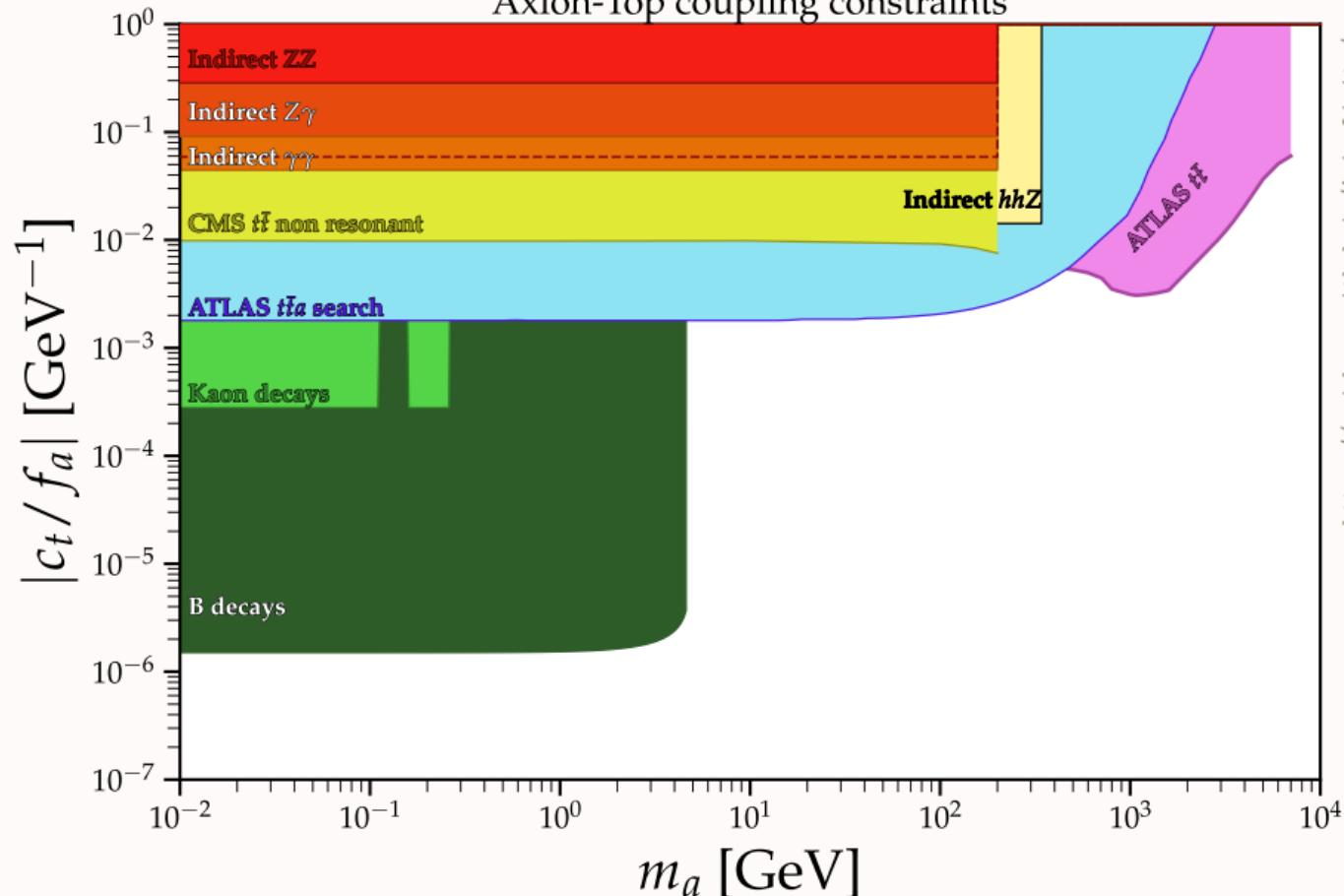
ALPs at Colliders (LHC)



<https://cajohare.github.io/AxionLimits/>



Axion-Top coupling constraints



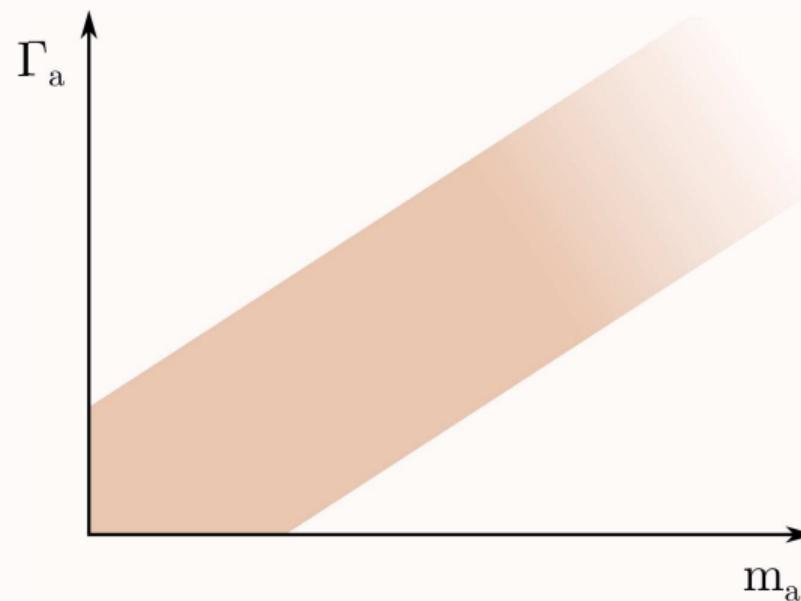
<https://cajohare.github.io/AxionLimits/>
Esser, Madigan, (Salas-Bernardez), Sanz, Ubiali
2303.17634, 2404.08062

Collider probes of the ALP parameter space

Motivation

- ▶ tree-level access to **couplings to heavy SM particles** (W, Z, h, t)
- ▶ access to **heavy ALPs** ($m_a \gtrsim \text{GeV}$)

Signatures

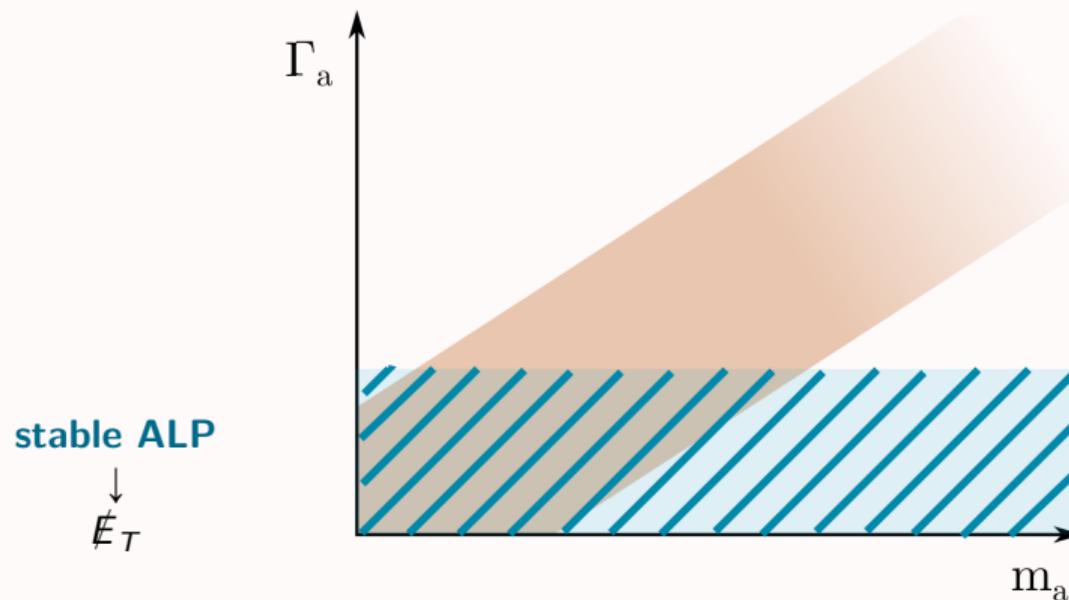


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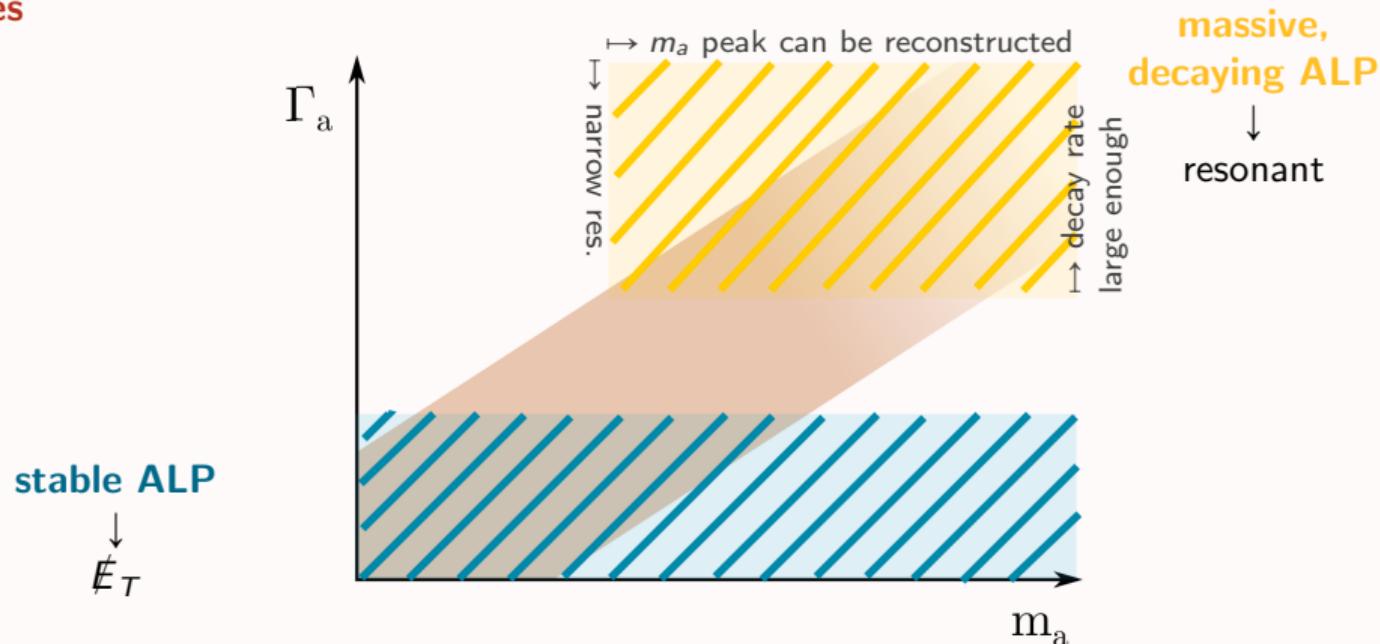


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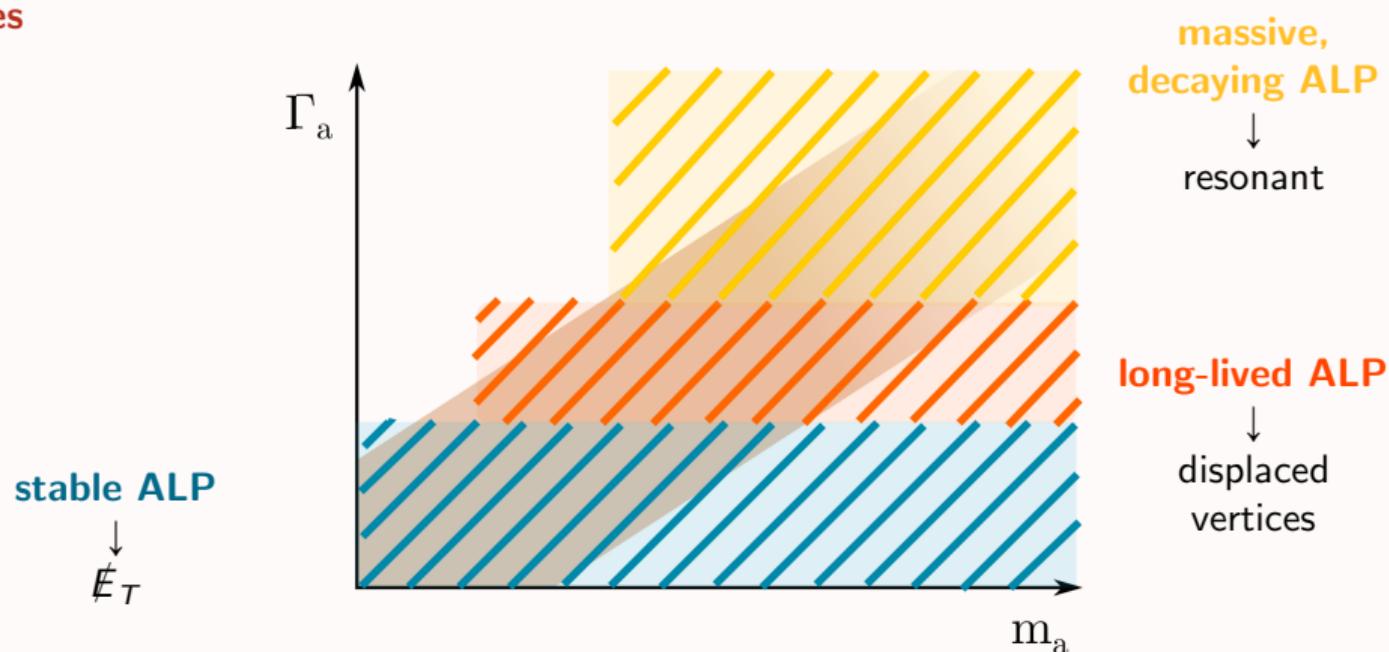


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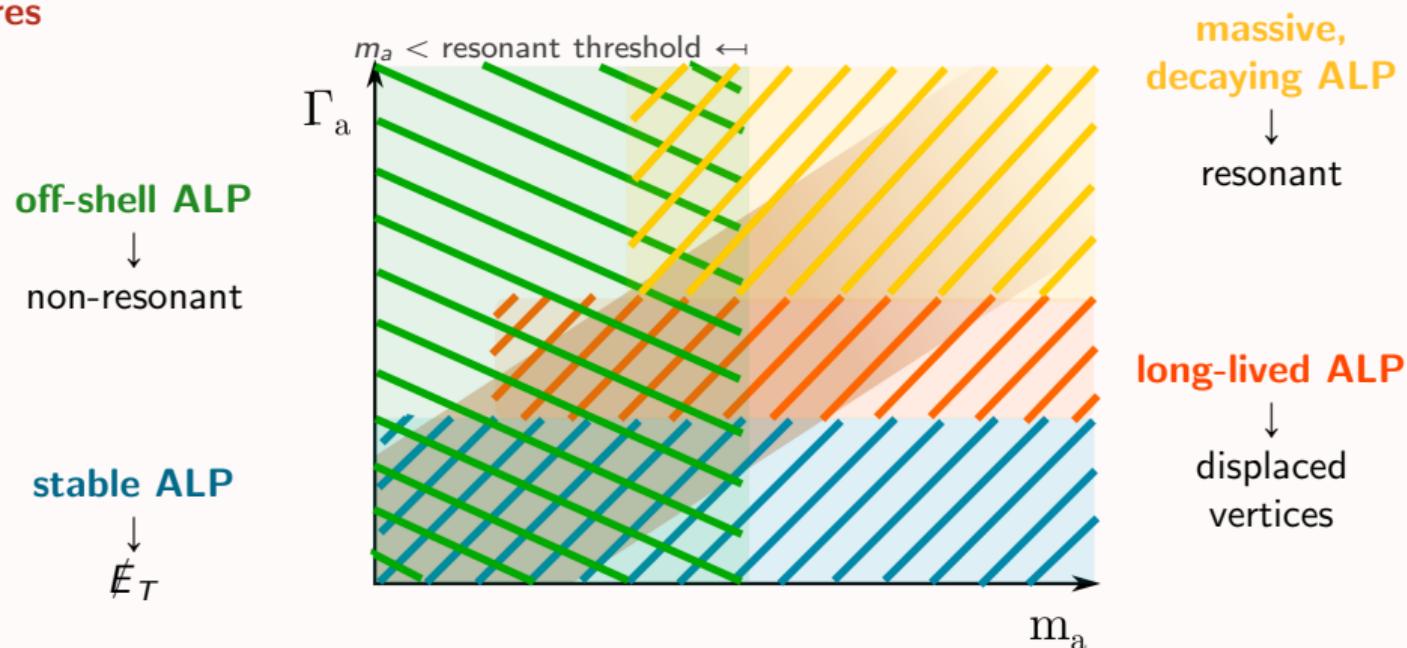


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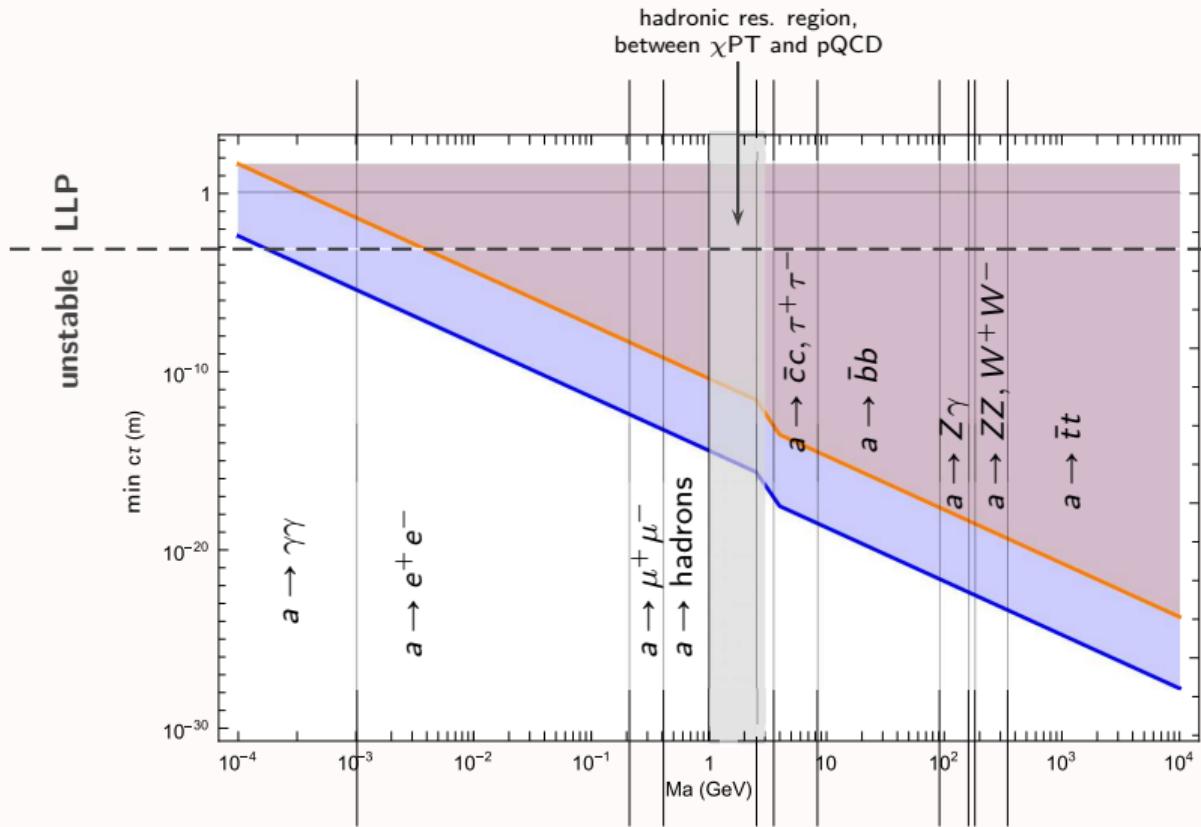
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Signatures



ALP decay modes and lifetime

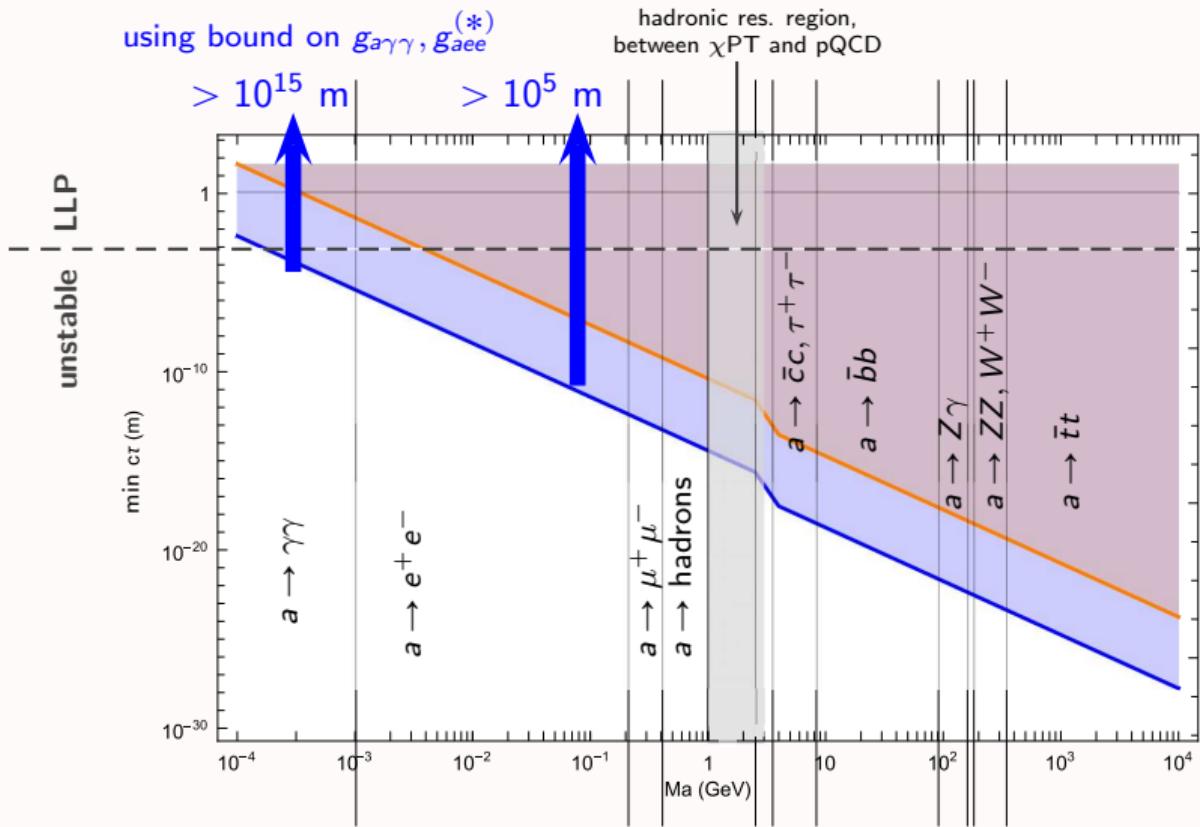


$$\Gamma_{a \rightarrow V_1 V_2} \sim m_a^3 \frac{C_j^2}{f_a^2}$$

$$\Gamma_{a \rightarrow \bar{f}f} \sim m_a m_f^2 \frac{C_f^2}{f_a^2}$$

$\text{--- } \frac{C_i}{f_a} < 10^3 \text{ TeV}^{-1}$
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ALP decay modes and lifetime



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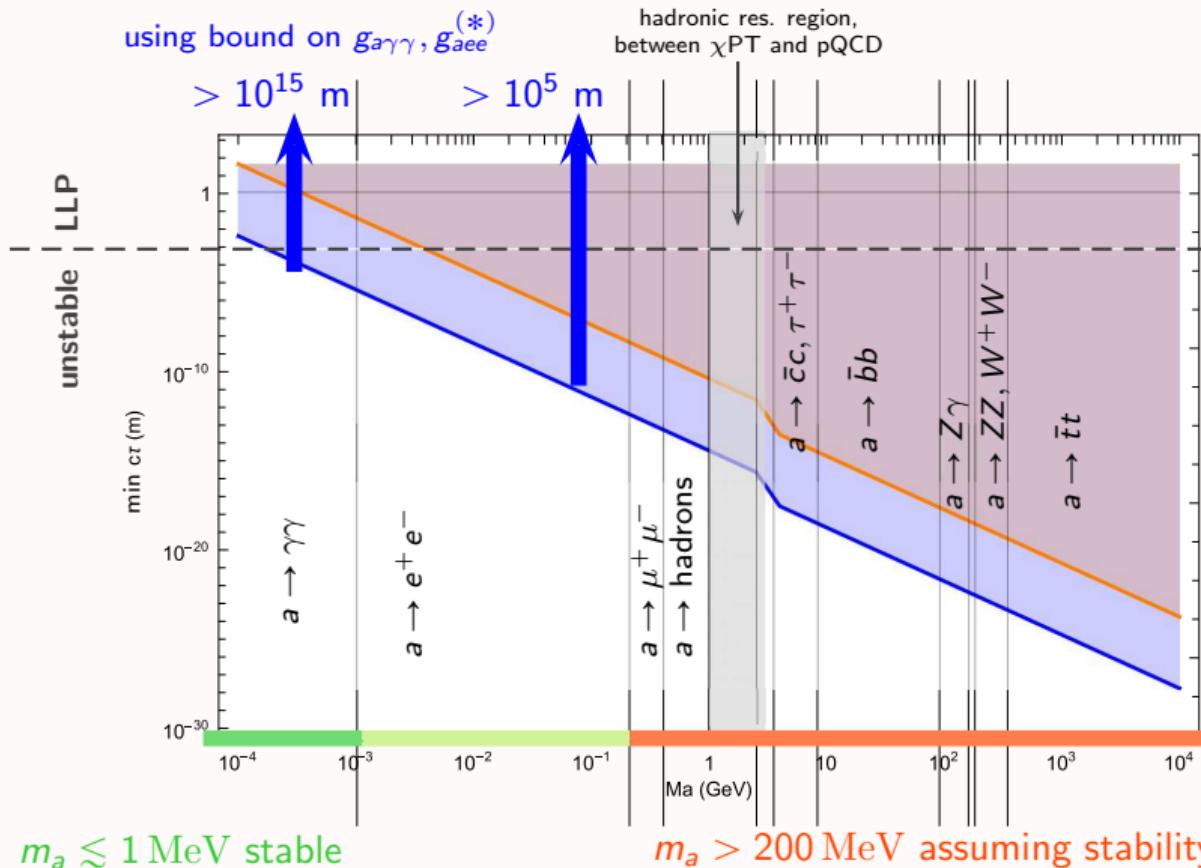
$$\Gamma_{a \rightarrow \bar{f}f} \sim m_a m_f^2 \frac{C_f^2}{f_a^2}$$

unstable LLP

$\frac{C_i}{f_a} < 10^3 \text{ TeV}^{-1}$

$\frac{C_i}{f_a} < 10 \text{ TeV}^{-1}$

ALP decay modes and lifetime

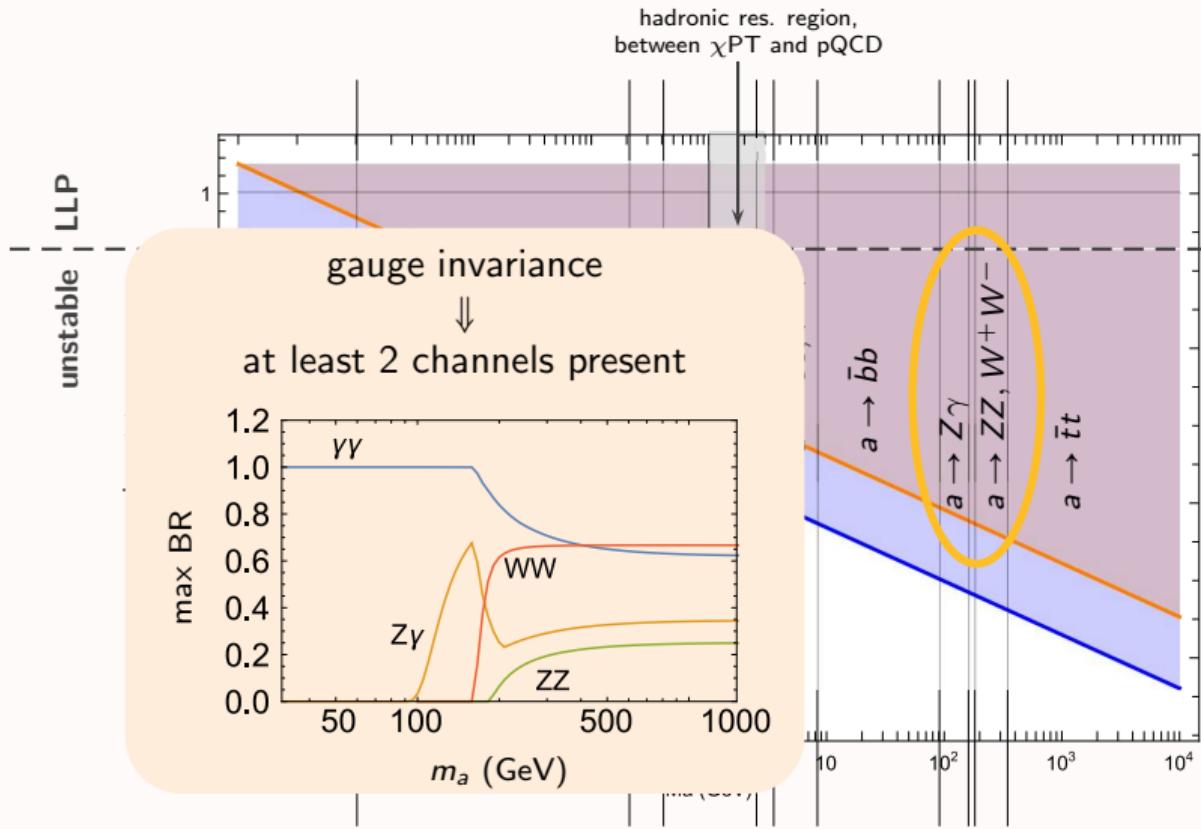


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- $\frac{C_i}{f_a} < 10^3 \text{ TeV}^{-1}$
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ALP decay modes and lifetime



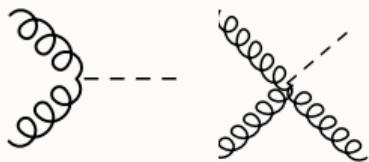
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blue line: $\frac{C_i}{f_a} < 10^3 \text{ TeV}^{-1}$

orange line: $\frac{C_i}{f_a} < 10 \text{ TeV}^{-1}$

ALP at LHC: main production modes

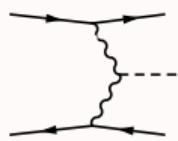


$gg \rightarrow a(g)$

$C_{\tilde{G}}$



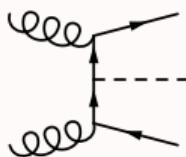
$q\bar{q} \rightarrow Va, V = Z, W^\pm, \gamma \quad C_{\tilde{B}}, C_{\tilde{W}}$



$q\bar{q} \rightarrow q\bar{q}a$

$C_{\tilde{B}}, C_{\tilde{W}}, C_{\tilde{G}}$

also: light-by-light



$gg \rightarrow \bar{t}ta$

C_f

ALP at LHC: main production modes

Depending on ALP mass: production via **decays of SM** states.

$$Z \rightarrow a\gamma$$

$$\textcolor{teal}{C}_{\tilde{B}}, \textcolor{red}{C}_{\tilde{W}}$$

Depending on presence of flavor violating couplings, or at 1-loop:

$$\psi_1 \rightarrow a\psi_2 \quad \textcolor{magenta}{C}_f, \textcolor{red}{C}_{\tilde{W}}$$

$$\psi_1 \rightarrow a\psi_2\gamma \quad \textcolor{magenta}{C}_f, \textcolor{red}{C}_{\tilde{W}}$$

$$M_1 \rightarrow aM_2 \quad \textcolor{magenta}{C}_f, \textcolor{green}{C}_{\tilde{G}}, \textcolor{red}{C}_{\tilde{W}}, \textcolor{teal}{C}_{\tilde{B}} \quad M_1, M_2 \text{ mesons, e.g. } B \rightarrow aK, K \rightarrow a\pi \dots$$

$$M \rightarrow a\gamma \quad \textcolor{magenta}{C}_f, \textcolor{green}{C}_{\tilde{G}}, \textcolor{red}{C}_{\tilde{W}}, \textcolor{teal}{C}_{\tilde{B}}$$

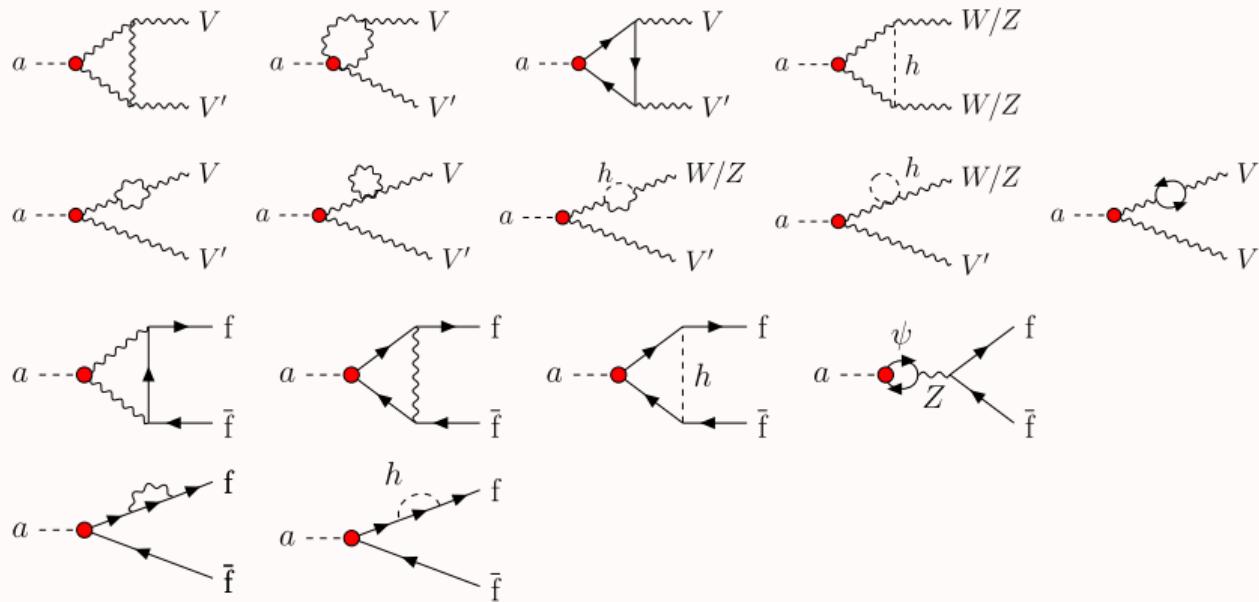
👎 very rich ALP phenomenology in **flavor physics**, not touched upon here

ALP EFT at 1-loop

in general, large “mixing” among coefficients at 1-loop:

each ALP coupling receives loop corrections from most ALP parameters

Bonilla,IB,Gavela,Sanz 2107.11392
Bauer,Neubert,Thamm 1708.00443
Bauer,Neubert,Renner, Schnubel,Thamm
2012.12272

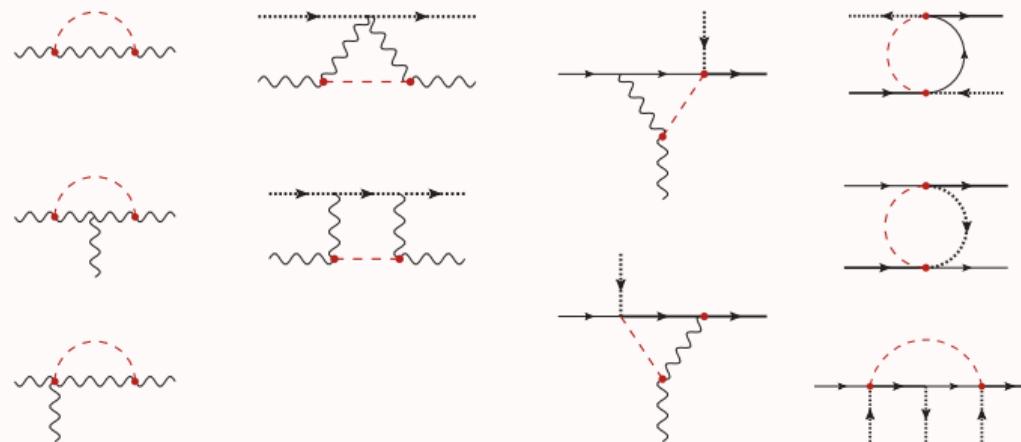


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dim-5 ALP operators also mix into dim-6 SMEFT ones with $\Lambda = 4\pi f_a$

Galda, Neubert, Renner 2105.01078

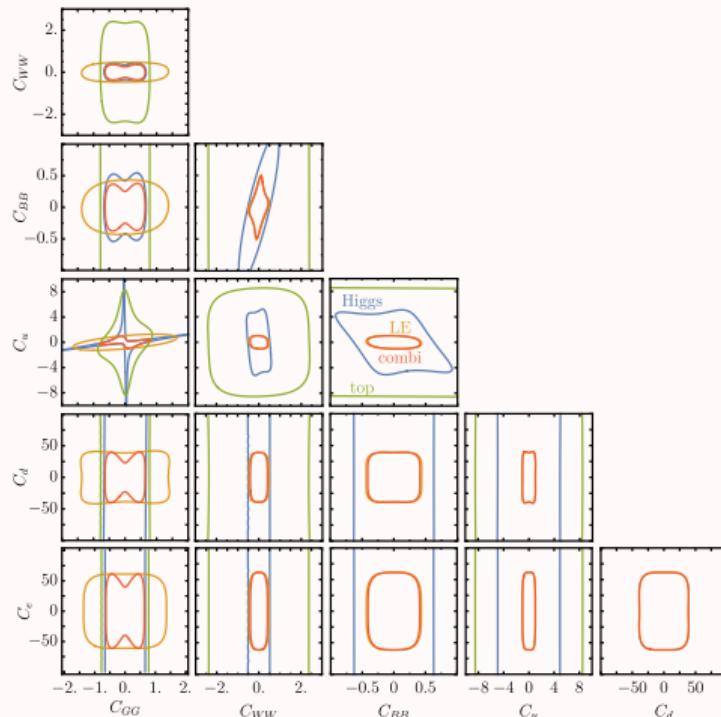


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Galda,Neubert,Renner 2105.01078



Biekötter,Fuentes-Martin, Galda,Neubert 2307.10372

Collider signals of flavor conserving, dim-5 couplings

incomplete list! omitting Higgs. flavor viol., ATLAS/CMS

Stable

- ▶ mono-Z, mono-W, mono- γ , mono-jet, di-jet

Mimasu,Sanz 1409.4792, IB+ 1701.05379, Haghight+ 2006.05302,
Haisch+ 2107.12839, Esser+ 2303.17634, Blasi+ 2311.16048,
Hosseini,Najafabadi 2408.11588, Ghebretinsae+ 2203.01734,
Ebadi+ 1901.03061, Rygaard+ 2306.08686, Bauer+ 1708.00443, 1808.10323

Unstable

light

- ▶ $pp \rightarrow W/Z/\gamma a, a \rightarrow \gamma\gamma$ resonant in pp
- ▶ $\gamma\gamma \rightarrow a \rightarrow \gamma\gamma$ resonant in Pb-Pb
- ▶ $q\bar{q} \rightarrow W/Z/\gamma a, a \rightarrow \gamma\gamma$
- ▶ $pp \rightarrow a \rightarrow \tau\tau, \mu\mu, c\bar{c}(D)$

Jäckel+ 1212.3620
Mariotti+ 1710.01743, 1810.09452 Knapen+ 1607.06083, 1709.07110
Baldenegro+ 1803.10835 Jäckel,Spannowsky 1509.00476
Wang+ 2102.01532, 2106.07018 Cheung+ 2402.10550
Cacciapaglia+ 1710.11142, 2106.12615

Unstable

heavy

- ▶ $pp \rightarrow aV_1 \rightarrow V_1 V_2 V_3$ ($V = W/Z/\gamma$) resonant
- ▶ $pp \rightarrow a \rightarrow t\bar{t}$ resonant
- ▶ $gg \rightarrow a^* \rightarrow VV', \bar{t}t$ non-resonant
- ▶ VBS non-resonant

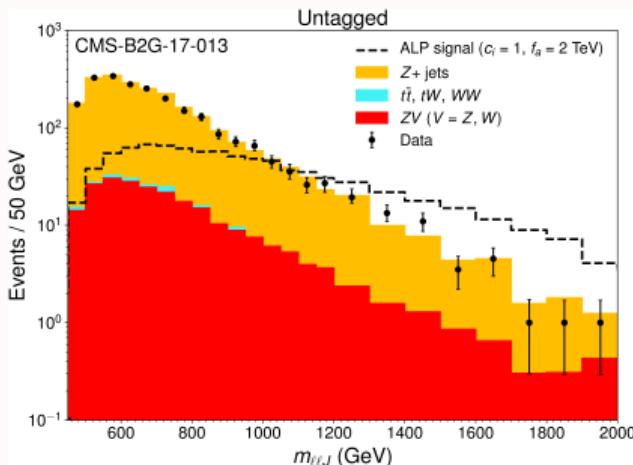
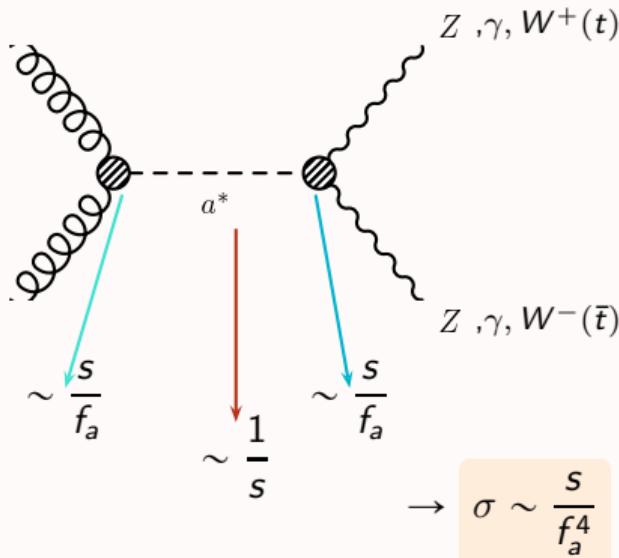
Craig,Hook,Kasko 1805.06538
Anuar+ 2404.19014, Aiko+ 2401.13323

Gavela+ 1905.12953 Carrá+ 2106.10085,
Flórez+ 2101.11119, Bonilla,IB+ 2202.03450

Non-resonant ALP signals at LHC

ZZ, $\gamma\gamma$, $t\bar{t}$: Gavela, No, Sanz, Troconiz 1905.12953, CMS PAS B2G-20-013 2111.13669
WW, $Z\gamma$: Carrá, Goumarre, Gupta, Heim, Heinemann, Küchler, Meloni, Quilez, Yap 2106.10085

ALP off-shell for $m_a \ll m_1 + m_2 \leq \sqrt{s}$ “too light to be resonant”

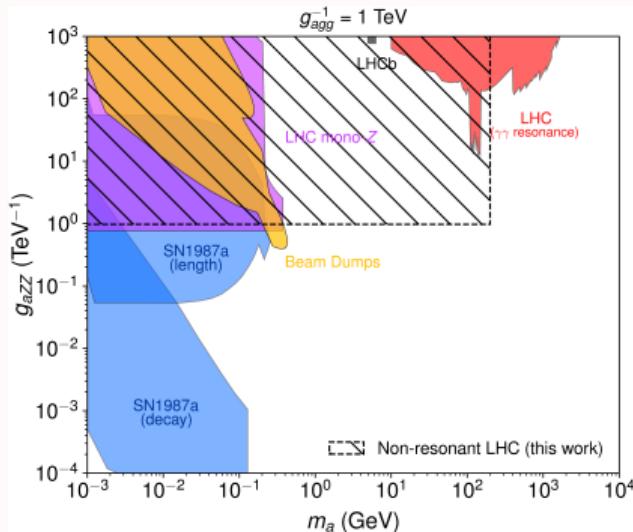
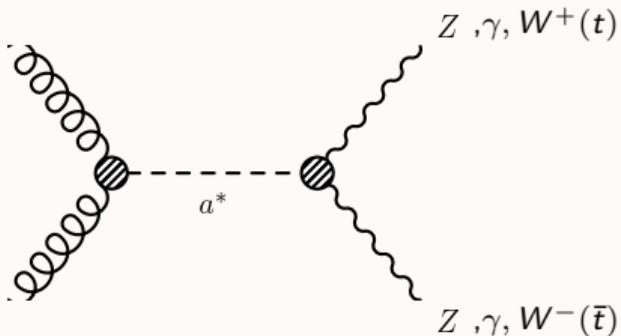


independent of m_a, Γ_a

Non-resonant ALP signals at LHC

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ALP off-shell for $m_a \ll m_1 + m_2 \leq \sqrt{s}$ “too light to be resonant”



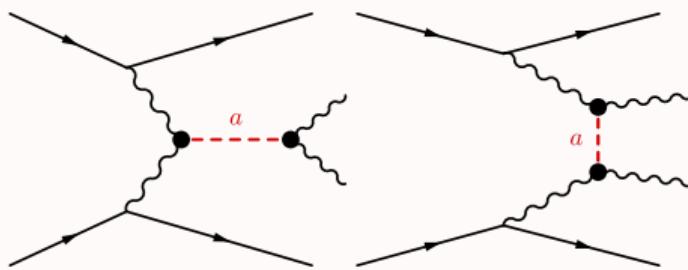
puts a constraint on $(g_{aGG} \times g_{aVV})$ product
for g_{aGG} not too small, competitive bounds on g_{aVV}

Non-resonant searches in VBS

apply same principle to Vector Boson Scattering

- independent of g_{aGG} (if pure ALP signal dominates, adding $C_{\tilde{B}}$ does not worsen bounds)
- a nice playground with several final states constraining the same 2 couplings

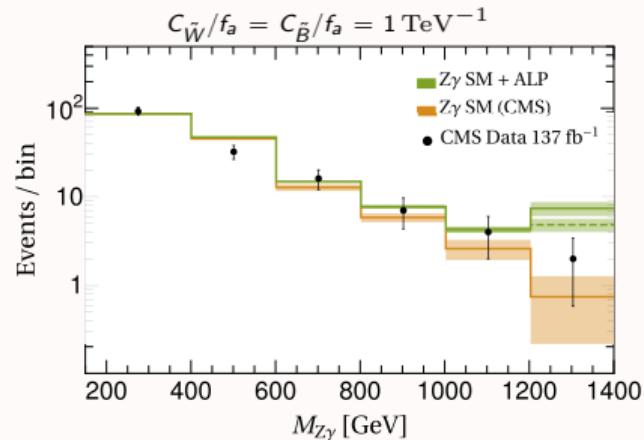
Bonilla, IB, Machado-Rodríguez, Trocóniz 2202.03450



$$\sigma = \sigma_{SM} + \sigma_{int.}/f_a^2 + \sigma_{ALP}/f_a^4$$

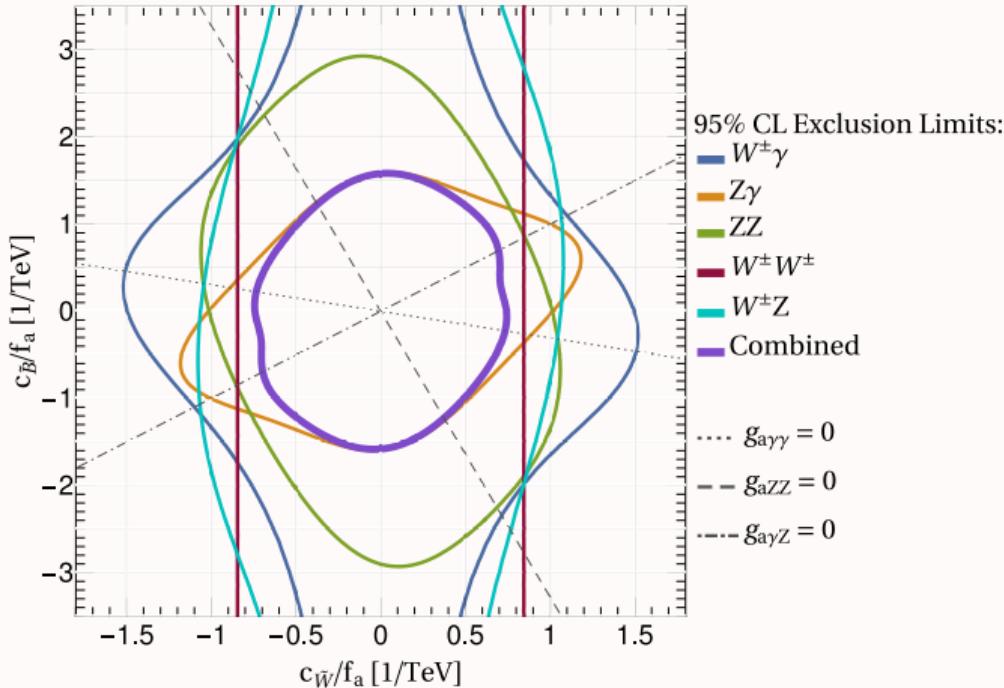
$$\sigma_{int.} = C_{\tilde{B}}^2 \sigma_{B2} + C_{\tilde{W}}^2 \sigma_{W2} + C_{\tilde{B}} C_{\tilde{W}} \sigma_{WB}$$

$$\sigma_{ALP} = C_{\tilde{B}}^4 \sigma_{B4} + C_{\tilde{W}}^4 \sigma_{W4} + C_{\tilde{B}}^2 C_{\tilde{W}}^2 \sigma_{W2B2} + C_{\tilde{B}}^3 C_{\tilde{W}} \sigma_{B3W} + C_{\tilde{B}} C_{\tilde{W}}^3 \sigma_{BW3}$$



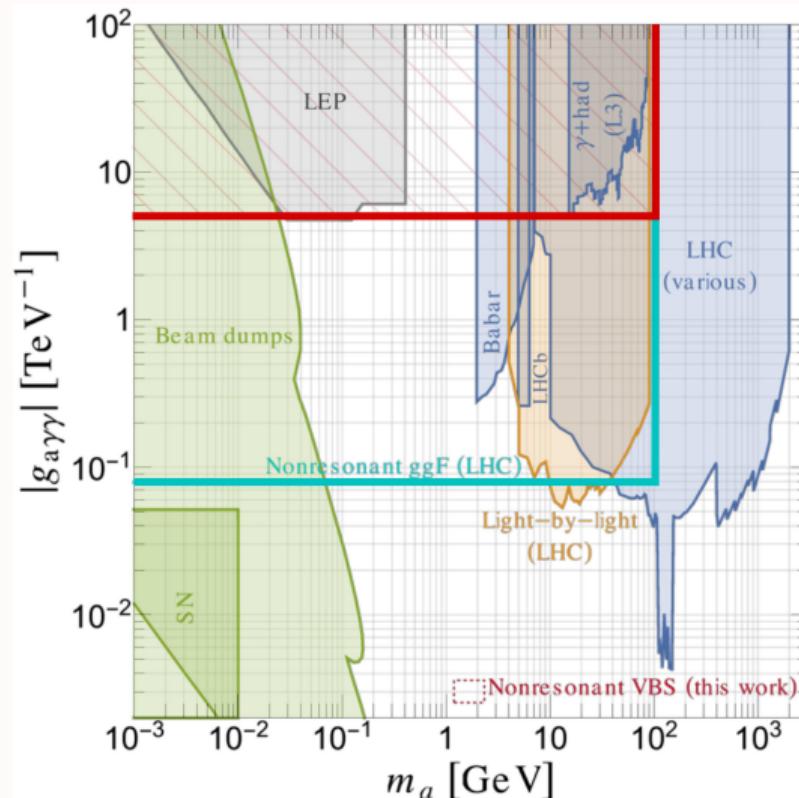
Non-resonant searches in VBS: Run 2 results

bounds extracted comparing to Run-2 CMS measurements



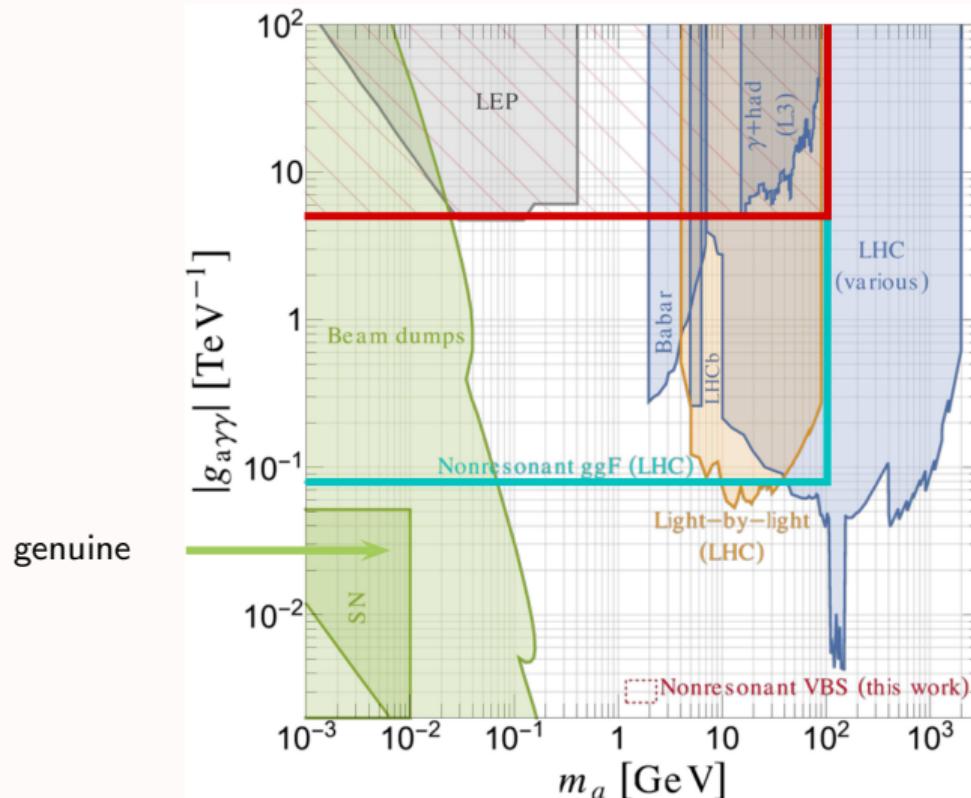
Comparing bounds, with a grain of salt

bounds typically represented in (m_a, g_{aXX}) , but hide different assumptions



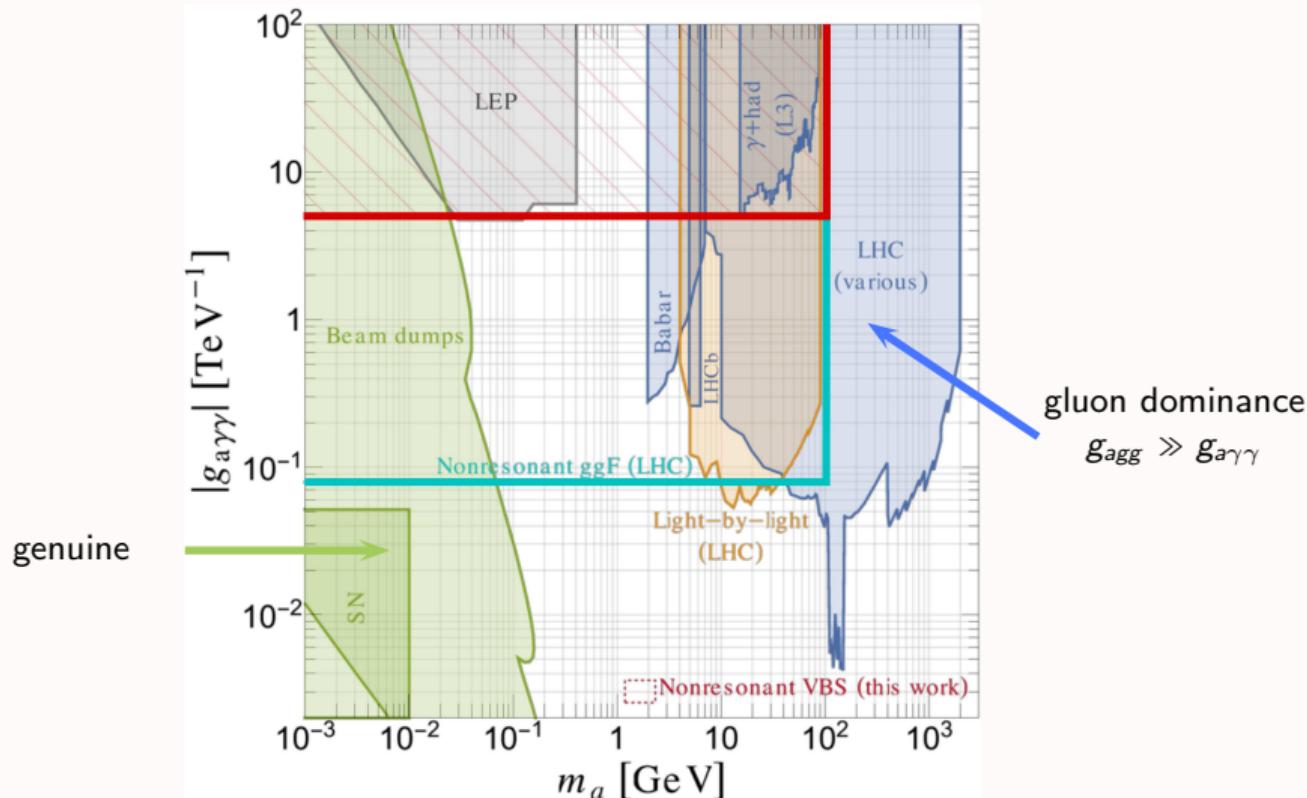
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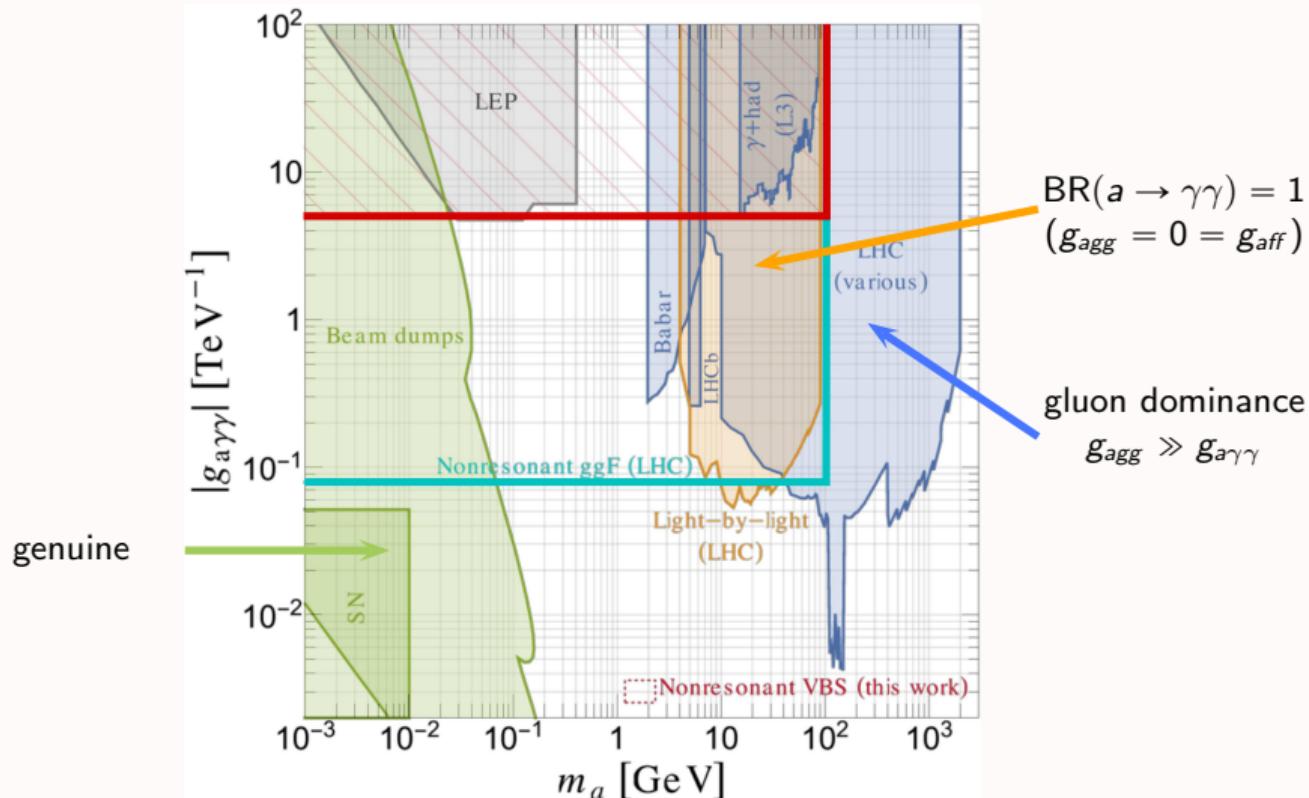
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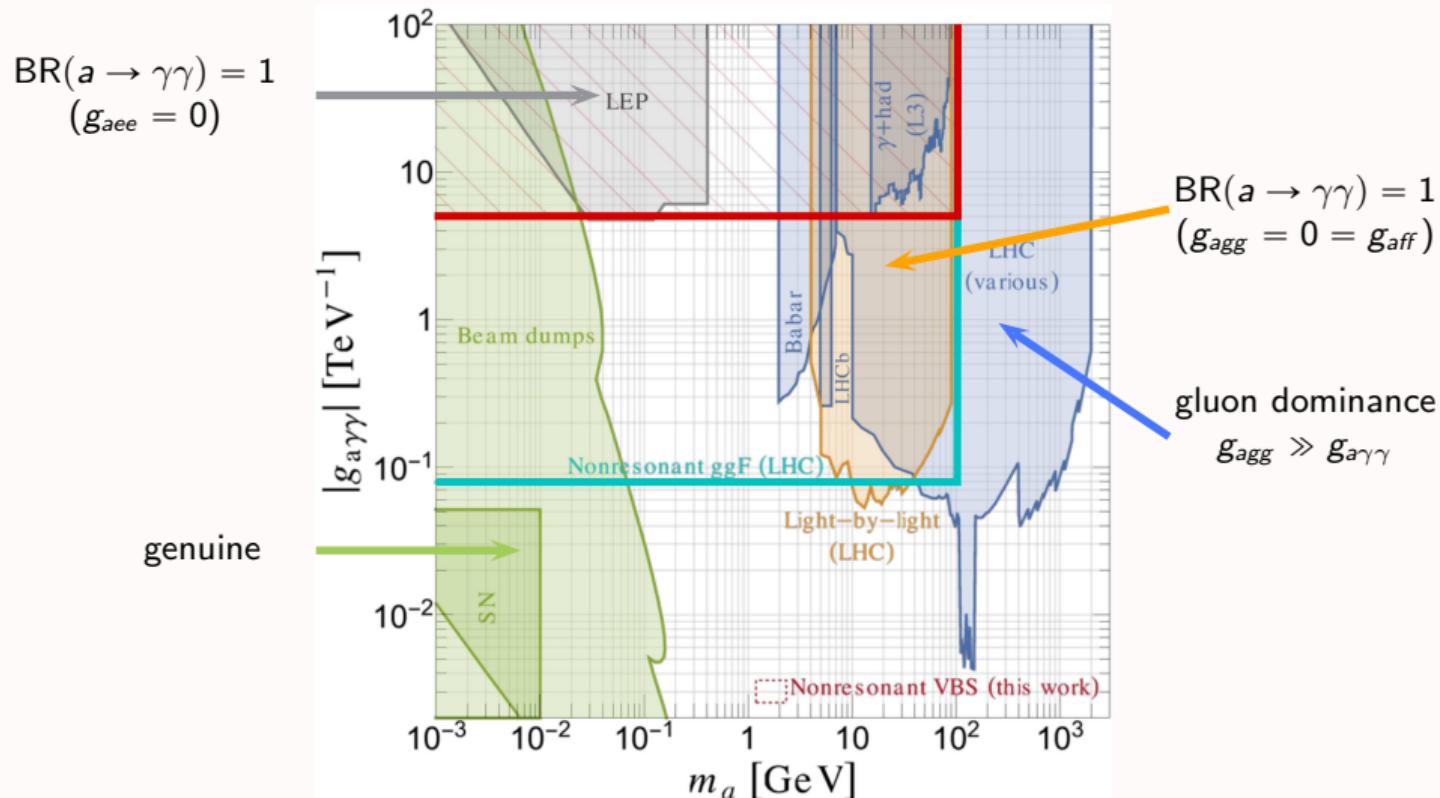
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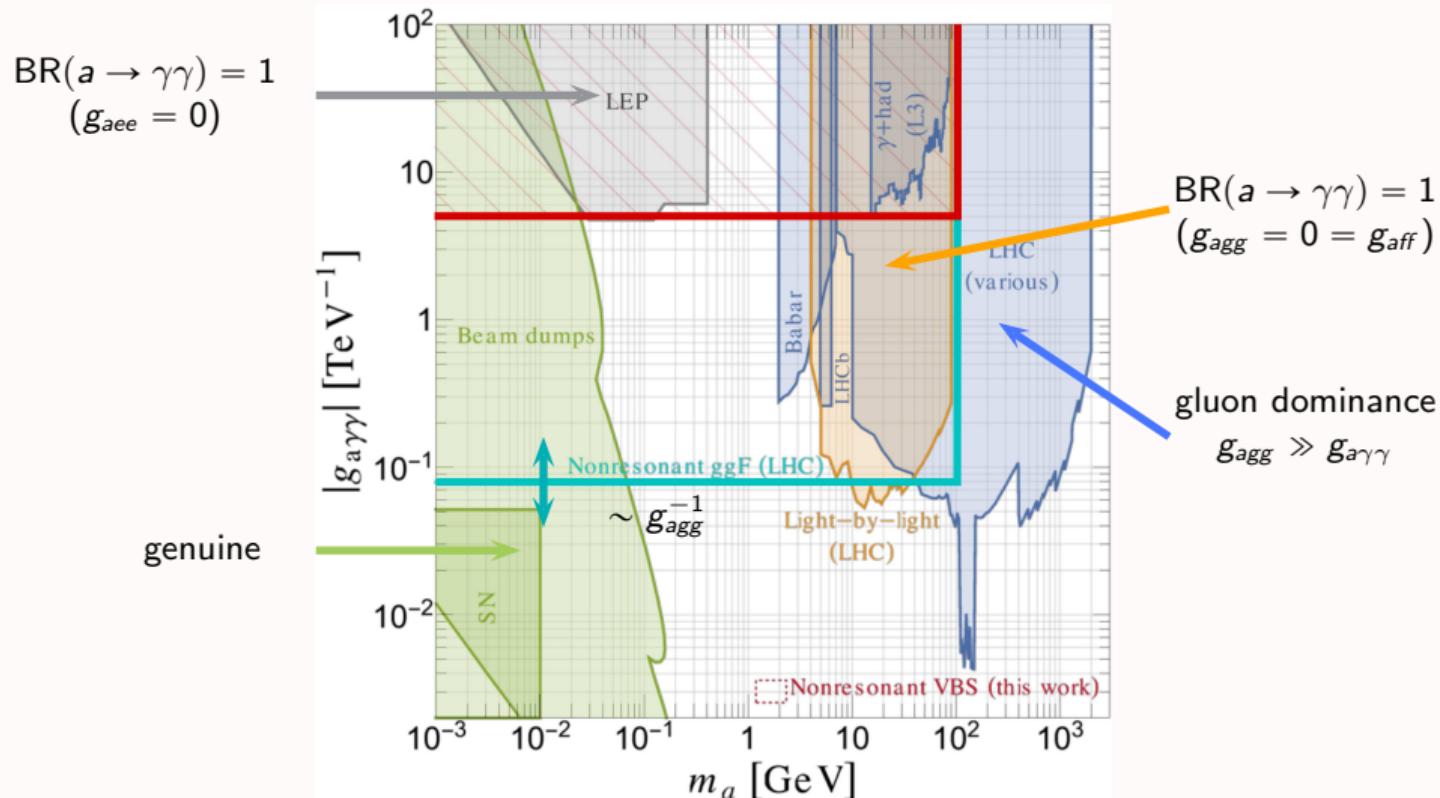
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bounds typically represented in (m_a, g_{aXX}) , but hide different assumptions



Unitarity constraints on ALP couplings

How much can we rely on s enhancements? Does the EFT stay valid?

IB, Éboli, González-García 2106.05977

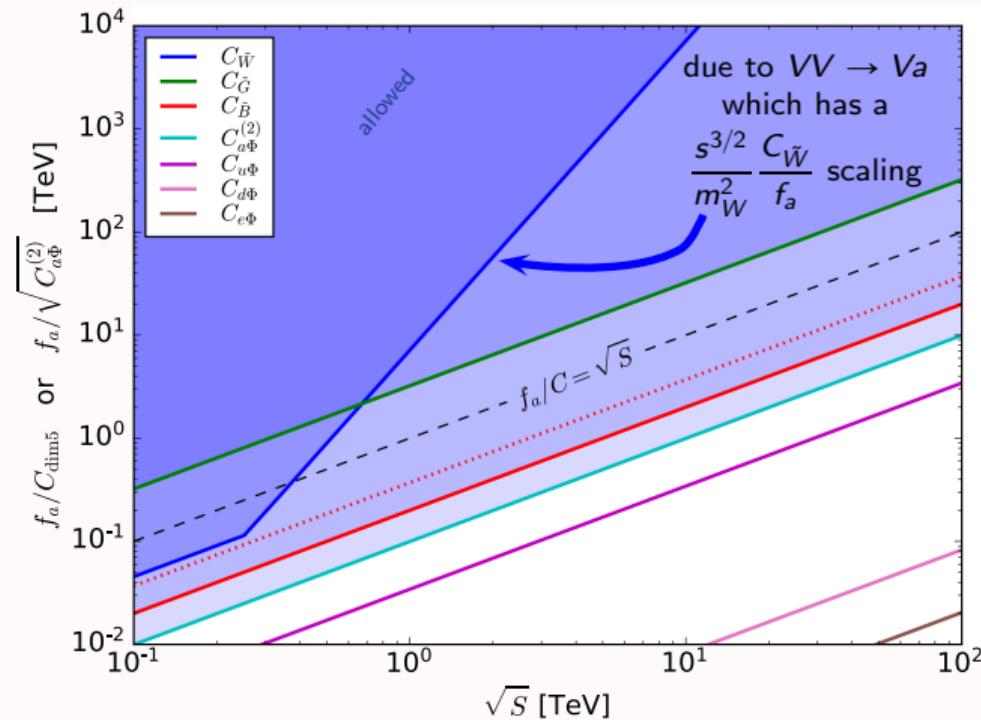
perturbative unitarity
requires

$$|T^J| \sim \beta \frac{\sqrt{s} C_i}{f_a} + \dots \leq 1$$

β some constant,
 $\dots =$ subleading orders in s



only **colored regions**
are physical



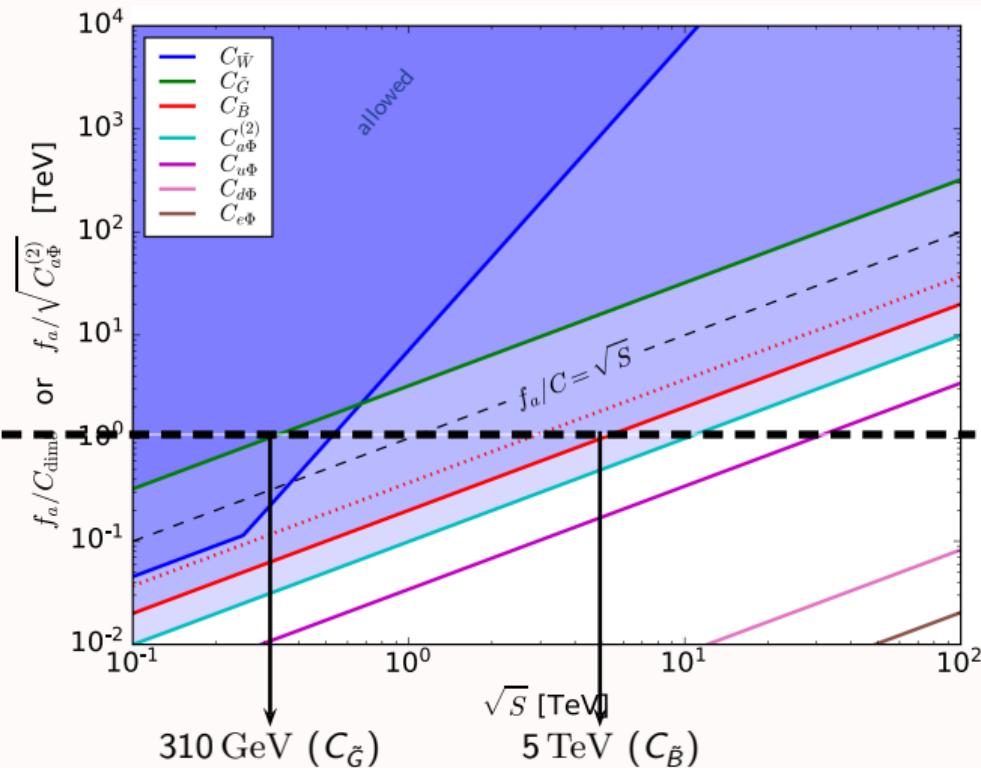
Unitarity constraints on ALP couplings

How much can we rely on s enhancements? Does the EFT stay valid?

IB, Éboli, González-García 2106.05977

an EFT with
 $f_a/C_i = 1 \text{ TeV}$

requires NP
at most at



Unitarity constraints on ALP couplings

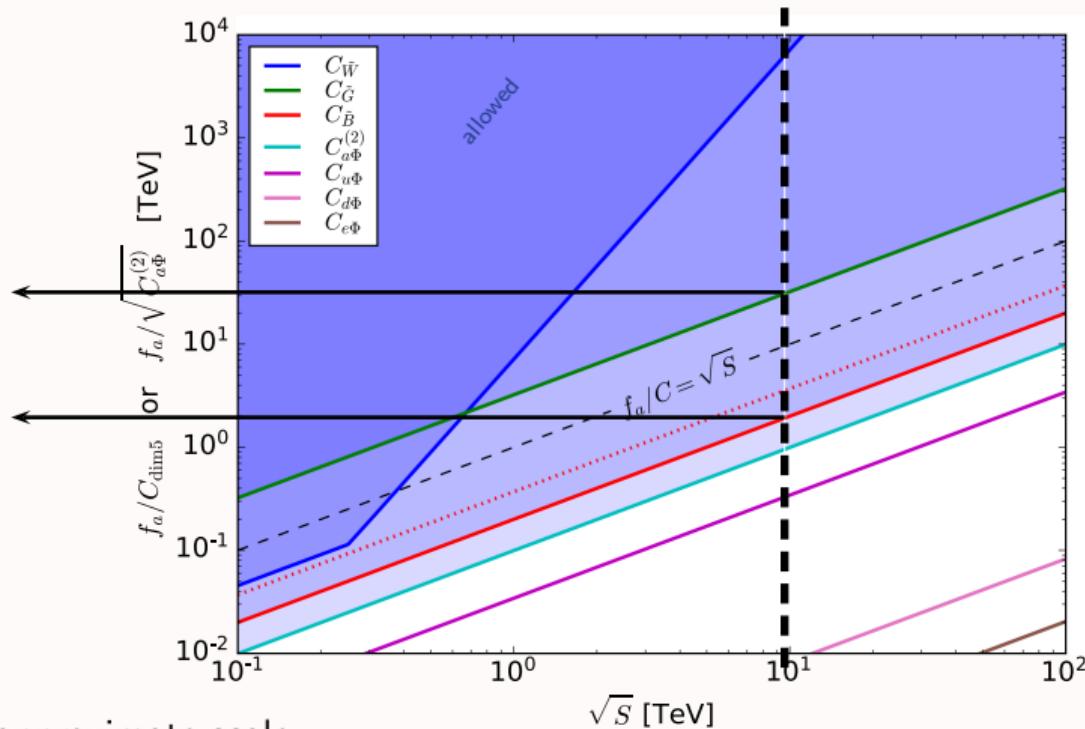
How much can we rely on s enhancements? Does the EFT stay valid?

IB, Éboli, González-García 2106.05977

a measurement at
 $\sqrt{s} \simeq 10$ TeV
can only probe:

$$f_a/C_{\tilde{G}} > 32 \text{ TeV}$$

$$f_a/C_{\tilde{B}} > 2 \text{ TeV}$$



⚠ here: \sqrt{s} approximate scale

ALP EFT to higher orders

Operator bases (with and without shift-symmetry) were built up to dim-8

Bonnefoy,Grojean,Kley 2206.04182
Grojean,Kley,Yao 2307.08563

dim-6 contains a unique shift-invariant operator $\frac{1}{f_a^2} \partial_\mu a \partial^\mu a H^\dagger H$

which introduces **couplings to the Higgs**: aah , $aahh$ and is the first operator with **2 ALPs**

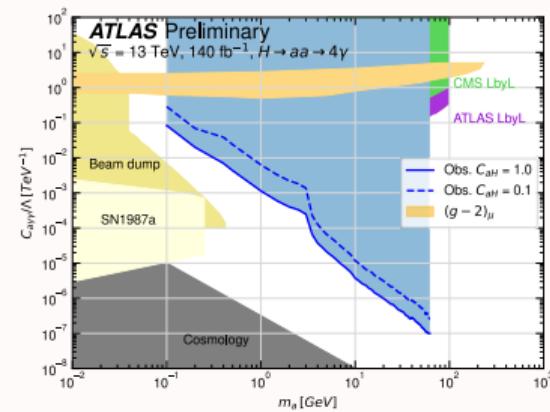
- rich phenomenology, incl. implications for ALP production in early universe

Bauer,Rostagni,Spinner
2207.05762

- for $m_a < m_h/2$, causes $h \rightarrow aa$
 $\Rightarrow h \rightarrow$ inv, stable ALP
 $h \rightarrow$ exotic channels ($4\gamma \dots$), unstable ALP

Bauer,Neubert,Thamm 1708.00443
ATLAS-CONF-2023-040

- enters meson decays as $M_1 \rightarrow M_2 aa$, $M^0 \rightarrow aa(\gamma)$



ALP EFT to (even) higher orders

dim-7 contains many more shift-invariant operators (5 w/o fermions), all with 1 ALP insertion

most notably, at this order the **aZh, aZh_h couplings** appear, from

$$\partial_\mu a (H^\dagger i \overleftrightarrow{D}_\mu H) H^\dagger H$$

▶ depending on m_a , it allows $h \rightarrow Za, a \rightarrow Zh$

IB et al 1701.05379, Bauer et al 1708.00443
Cheung,Ouseph 2402.05678

▶ mediates mono-Higgs $pp \rightarrow Z^* \rightarrow ah$ and ahh

▶ can induce non-resonant $pp \rightarrow a* \rightarrow hhZ$

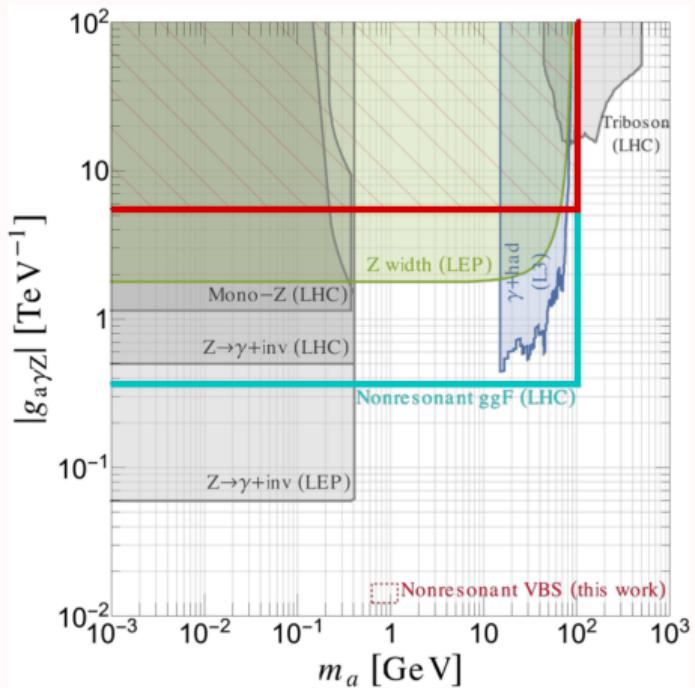
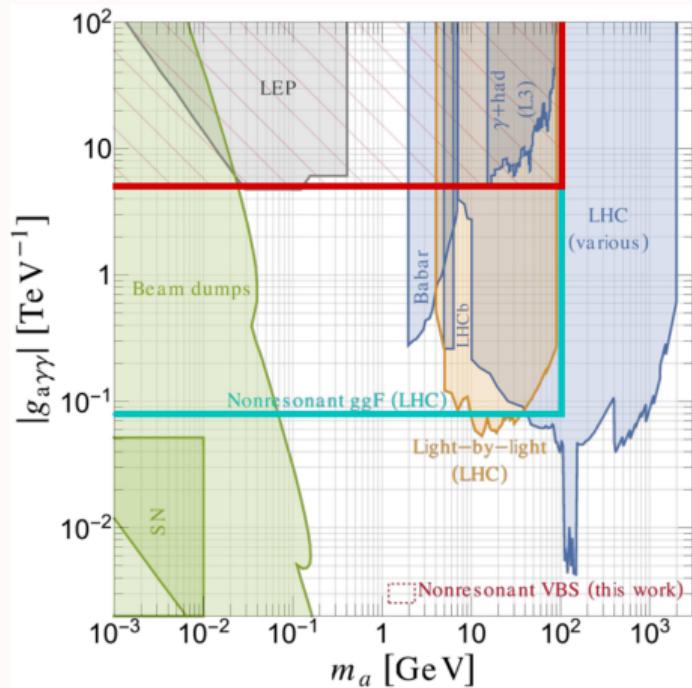
Esser, Madigan, Salas-Bernardez, Sanz, Ubiali 2404.08062

ALP EFT wrap-up

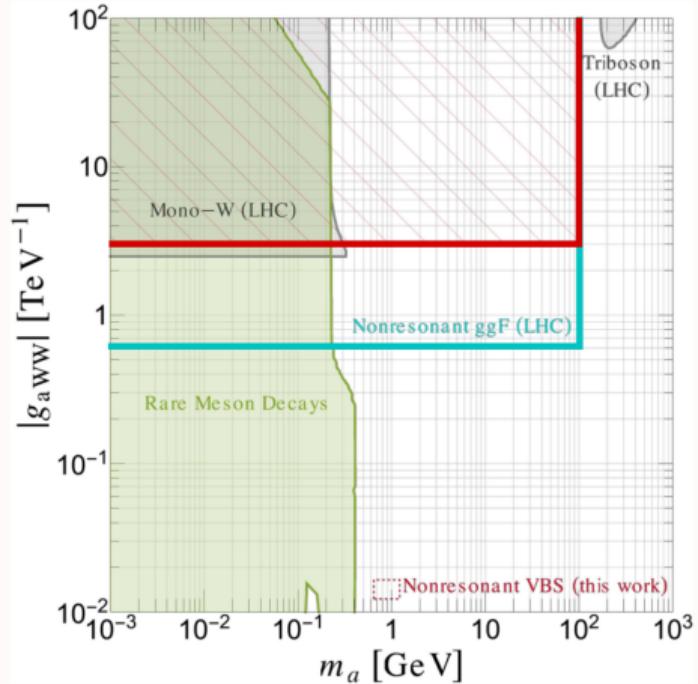
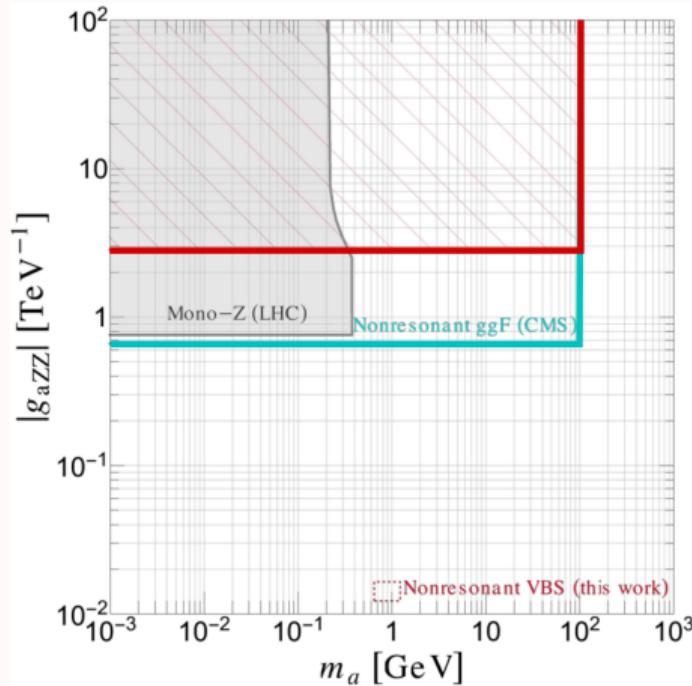
- ▶ ALPs are interesting! ubiquitous & discovery-friendly BSM/DM candidates
- ▶ a **very** rich phenomenology! thanks to wildly broad parameter space
- ▶ **ALP EFT** associated BSM sector integrated out
 - simple: limited # of parameters
 - non-trivial: shift-symmetry and anomalies complicate basis structure
 - interesting interplays at loop level
- ▶ **Colliders** crucial to probe **heavy** ALPs and couplings to **heavy** SM states
 - broad phenomenology, depending on mass and open decay channels
- ▶ **perturbative unitarity** considerations relevant for high-E (LHC) studies
 - if an ALP is discovered, give an upper limit to NP scale
- ▶ several colliders searches performed, many ideas applied.
 - non-resonant** signals in heavy final states particularly suited for ALPs

Backup slides

Bounds on ALP couplings

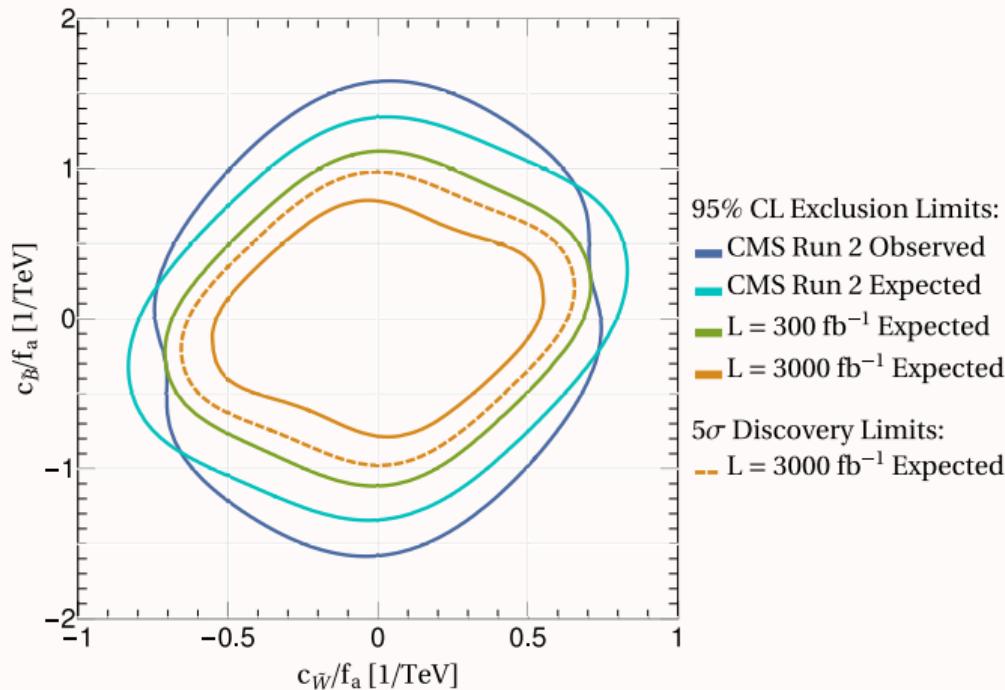


Bounds on ALP couplings

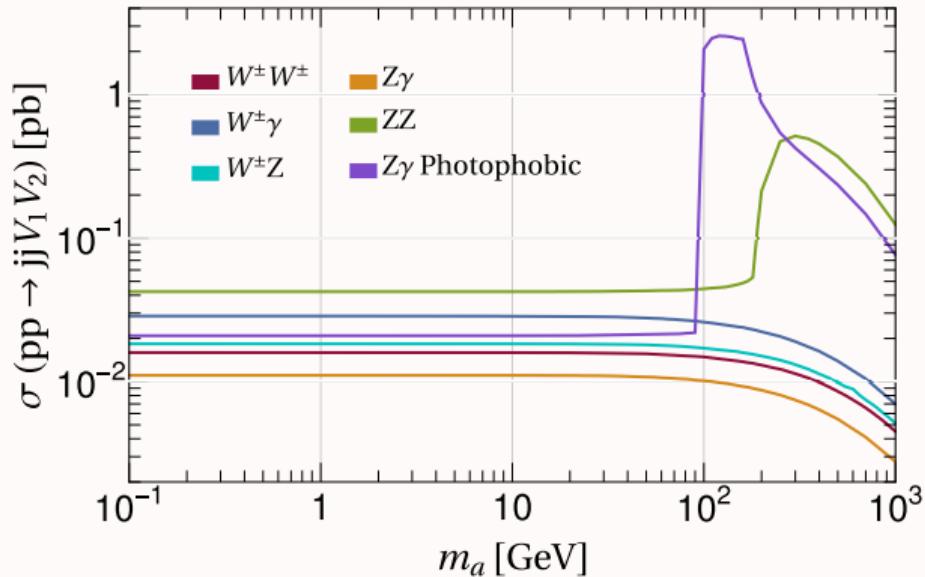


Non-resonant searches in VBS: projections

HL-LHC: sensitivity improves $\times 5 - 8$ on XS $\rightarrow \times 1.5 - 1.7$ on C_i/f_a



Dependence on ALP mass and width



- ▶ as long as $q^2 \gg m_a, \Gamma_a$, **independent** of exact values of mass and width
“reverse” of an EFT ($q^2 \gg m^2$ vs $q^2 \ll m^2$ limit)
- ▶ XS stable up until $m_a \lesssim 100$ GeV

Perturbative unitarity

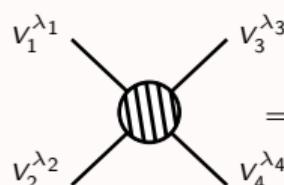
partial-wave decomposition for $2 \rightarrow 2$ scattering:

Jacob, Wick 1959

V_i = vector bosons or scalars

λ_i = helicities ($V: \lambda_i = 0, \pm 1$, $S: \lambda_i \equiv 0$), $\lambda = \lambda_1 - \lambda_2$, $\mu = \lambda_3 - \lambda_4$

T^J = amplitude for J -wave scattering



$$= 16\pi \sum_J (2J+1) \sqrt{1 + \delta_{V_1 V_2}^{\lambda_1 \lambda_2}} \sqrt{1 + \delta_{V_3 V_4}^{\lambda_3 \lambda_4}} e^{i(\lambda-\mu)\phi} d_{\lambda\mu}^J(\theta) T^J(V_1^{\lambda_1} V_2^{\lambda_2} \rightarrow V_3^{\lambda_3} V_4^{\lambda_4})$$

unitarity = $|T^J(V_1^{\lambda_1} V_2^{\lambda_2} \rightarrow V_1^{\lambda_1} V_2^{\lambda_2})| \leq 1$ for $s \gg (M_1 + M_2)^2$

[defined for *elastic* scattering]

unitarity violation
= unphysical pred.

the theory is not valid: new dynamical **states** must be included
pert. expansion is not valid: entering a **non-perturbative** regime

in ALP EFT: $|T^J| \sim \left[C_i \frac{\sqrt{s}}{f_a} \right]^n \left[\frac{\sqrt{s}}{m_W} \right]^m$ becomes > 1 for large \sqrt{s} or (C_i/f_a)

Perturbative unitarity in ALP EFT

Calculation strategy

IB, Éboli, González-García 2106.05977
also: Corbett, Éboli, González-García 1411.5026, 1705.09294

1. compute partial waves for all possible $2 \rightarrow 2$ processes in large \sqrt{s} lim:

$$V_1 V_2 \rightarrow V_3 V_4$$

$$V_1 a \rightarrow V_2 a$$

$$V_1 V_2 \rightarrow aa$$

$$V_1 V_2 \rightarrow V_3 a$$

$$ha \rightarrow ha$$

$$hh \rightarrow aa$$

$$f_1 \bar{f}_2 \rightarrow Va$$

2. construct $T^{J=0}, T^{J=1}$ matrices in final states (particle and helicity) space
→ block-diagonal classifying processes by Q and color contraction
3. **diagonalize** T^J matrices → “overall” constraint on theory
4. apply elastic unitarity requirement $|t^J| \leq 1$ on each eigenvalue

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Constraints identified allowing all operators simultaneously.

- ▶ $O_{\tilde{W}}$ dominated by T^1 from $VV \rightarrow Va$, scaling as $C(\sqrt{s})^3/(f_a m_W^2)$
- ▶ $O_{\tilde{B}}, O_{\tilde{G}}$ dominated by T^0 from $VV \rightarrow VV, aa$, scaling as $(C\sqrt{s}/f_a)^2$
- ▶ O_{fH} dominated by $\bar{f}f \rightarrow Va$, scaling as $C\sqrt{s}/f_a$

Chirality-flip operators

one can introduce

$$O_{uH,ij} = \frac{ia}{f_a} (\bar{Q}_i \tilde{H} u_j) \quad O_{dH,ij} = \frac{ia}{f_a} (\bar{Q}_i H d_j) \quad O_{eH,ij} = \frac{ia}{f_a} (\bar{L}_i H e_j)$$

⚠ NOT shift-invariant! but related to O_f via EOM, e.g.

$$-O_{e,ij} = O_{eH,kj}(Y_e)_{ki} + O_{eH,ik}^\dagger(Y_e^\dagger)_{jk} + \frac{g'^2}{16\pi^2} O_{\tilde{B}} \delta_{ij}$$

$O_f \rightarrow O_{fH}$ trading always possible. $O_{fH} \rightarrow O_f$ only possible if

Chala, Guedes, Ramos,
Santiago 2012.09017

$$C_{eH} = A_e Y_e + Y_e B_e \quad C_{uH} = A_Q Y_u + Y_u B_u \quad C_{dH} = A_Q Y_d + Y_d B_d$$

with $A_f = A_f^T, B_f = B_f^T$.

- 👉 $\{O_{fH}\}$ as above have same # DOFs as $\{O_f\}$
- 👉 trading $O_{\tilde{G}}$ for fermions requires a combination of O_f and O_{fH} (expl. shift break)
- 👉 one can remove ALL $O_{\tilde{X}}$ from the basis, but must retain both O_f and O_{fH} terms