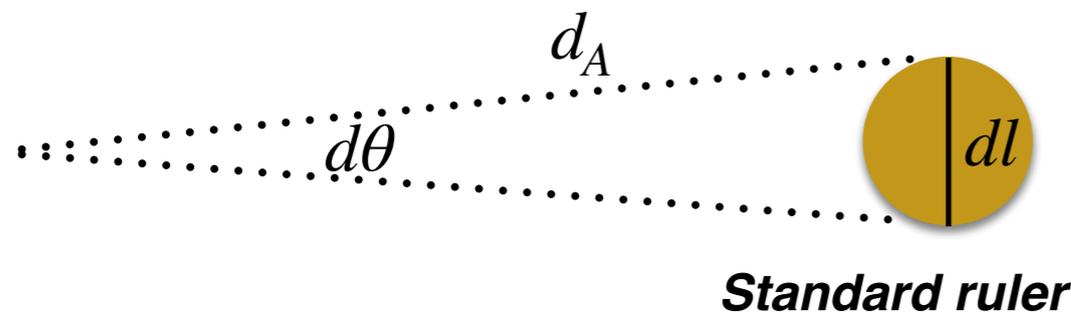


J. Lesgourgues

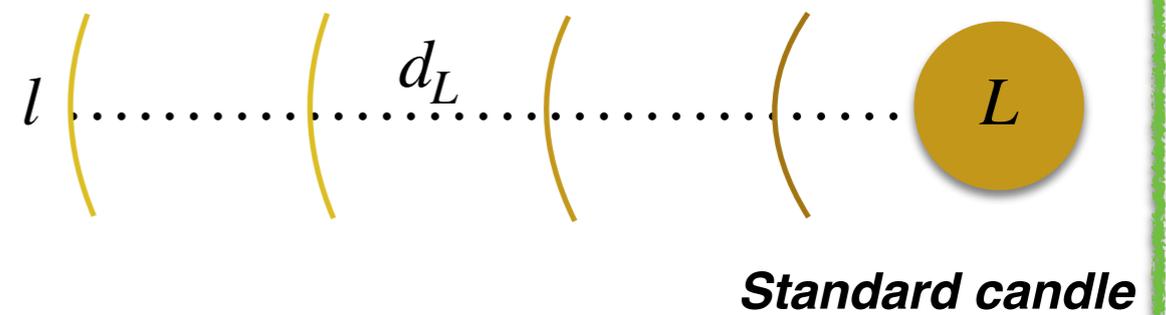
Institut für Theoretische Teilchenphysik und Kosmologie (TTK), RWTH Aachen University

Distances in cosmology

Angular diameter distance $d_A \equiv \frac{dl}{d\theta}$



Luminosity distance $d_L \equiv \sqrt{\frac{L}{4\pi l}}$



Relation between distances and redshift $d_L = a(t_0) (1 + z_e) f_k \left(\int_0^{z_e} \frac{c dz}{a(t_0) H(z)} \right) = (1 + z_e)^2 d_A$

↑
redshift $z =$ "look-back time"

Concordance cosmology

1992 - 2016: towards concordance cosmology:

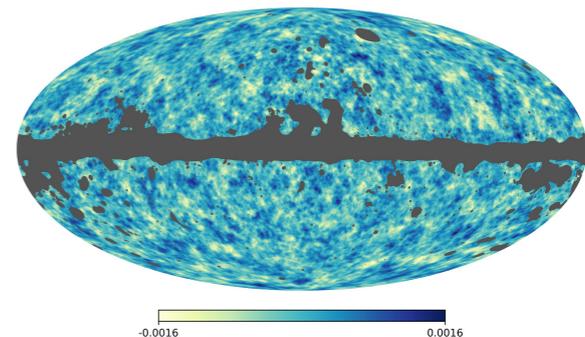
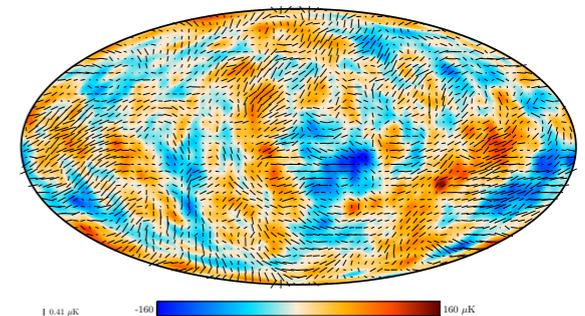
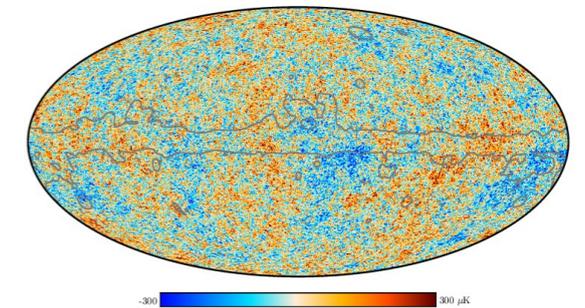
- Cosmic Microwave Background (CMB): maps for
 - temperature,
 - polarisation,
 - gravitational lensing.
- Big Bang Nucleosynthesis (BBN) & primordial elements
- Large Scale Structure of the universe (LSS):
 - Galaxy clustering
 - Cosmic shear (weak lensing)
- Cepheids and Supernovae luminosity

...

⇒ Λ CDM concordance model:

- General Relativity, QED, nuclear physics;
- inflation, baryons, Cold Dark Matter, cosm. const., photons, neutrinos;
- 7 free params. (6 after measurement of T_{CMB})

Planck maps



Discordance cosmology

2016 - 2012: towards discordance cosmology?

Hubble rate $H_0 = \frac{\dot{a}(t_0)}{a(t_0)} = 100 h$ km/s/Mpc

- CMB:

Planck 2018: $H_0 = 67.36 \pm 0.54$ km/s/Mpc

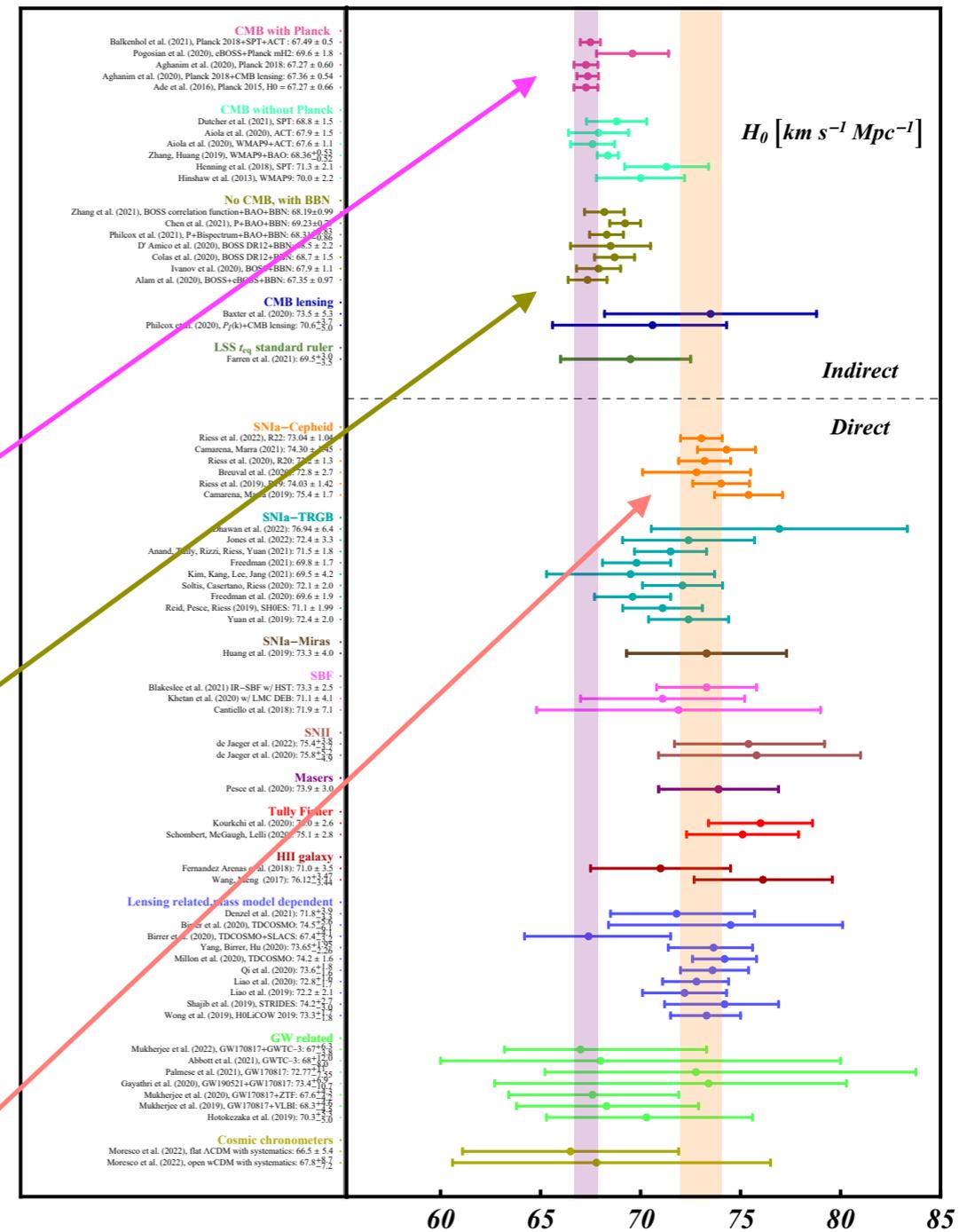
- Baryon Acoustic Oscillations (BAO):

BOSS+eBOSS+BBN: $H_0 = 67.35 \pm 0.97$ km/s/Mpc



- Supernovae + Cepheids:

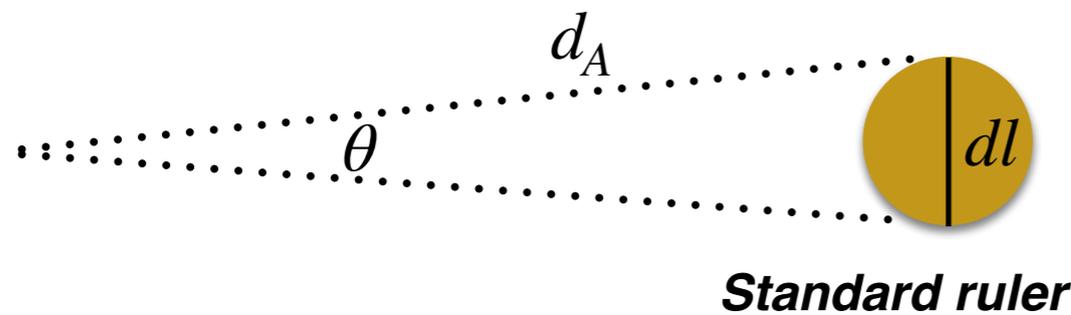
SH0ES 2022: $H_0 = 73.04 \pm 1.04$ km/s/Mpc



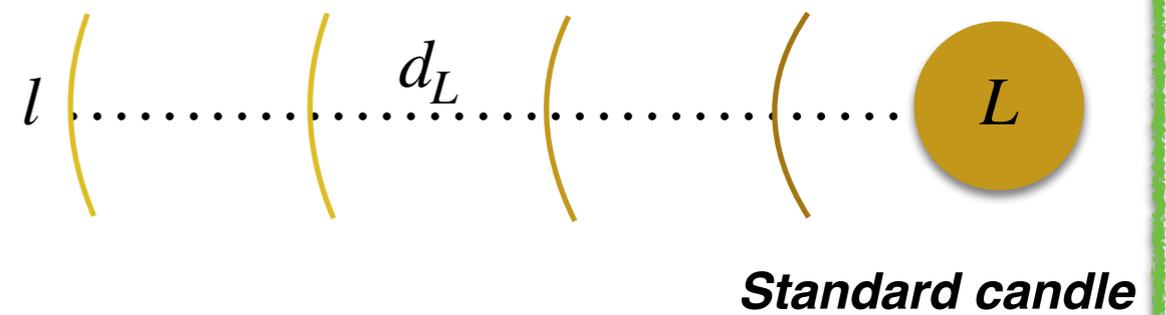
Riess et al. 22

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 redshift $z =$ "look-back time"

⇒ Measurement of H_0 by CMB/BAO: sound horizon as standard ruler: $d_A = d_s / \theta_s$

Foundations of the minimal cosmological model

Physics of CMB anisotropies and LSS:

- Einstein equations + Friedmann metric: $3H^2 = 8\pi G \rho$ and $\delta G_{\mu\nu} = 8\pi G \delta T_{\mu\nu}$
- Equations of motion:
 - linearised Boltzmann $\partial_t f_i(x^\mu, p^\nu) = C[f_1, f_2, \dots]$
 - or linearised fluid equations (continuity, Euler)
- Thomson scattering rate \Rightarrow ionisation fraction \Rightarrow basic QED, hydrogen atom
- Initial conditions: inflation \Rightarrow gaussian random field with nearly scale-invariant
2-point correlation function / power spectrum



CLASS, CAMB

2-point correlation function / **power spectrum** at any later time

\Rightarrow many features, incl. oscillations: $\cos(2\pi d_s / \lambda)$ (acoustic waves before $\gamma - b$ decoupling)

↖ ↗
wavelength

sound horizon = distance travelled by sound wave from BB till decoupling

Foundations of the minimal cosmological model

Λ CDM = 6-parameter fit
to ~5000 independent data points

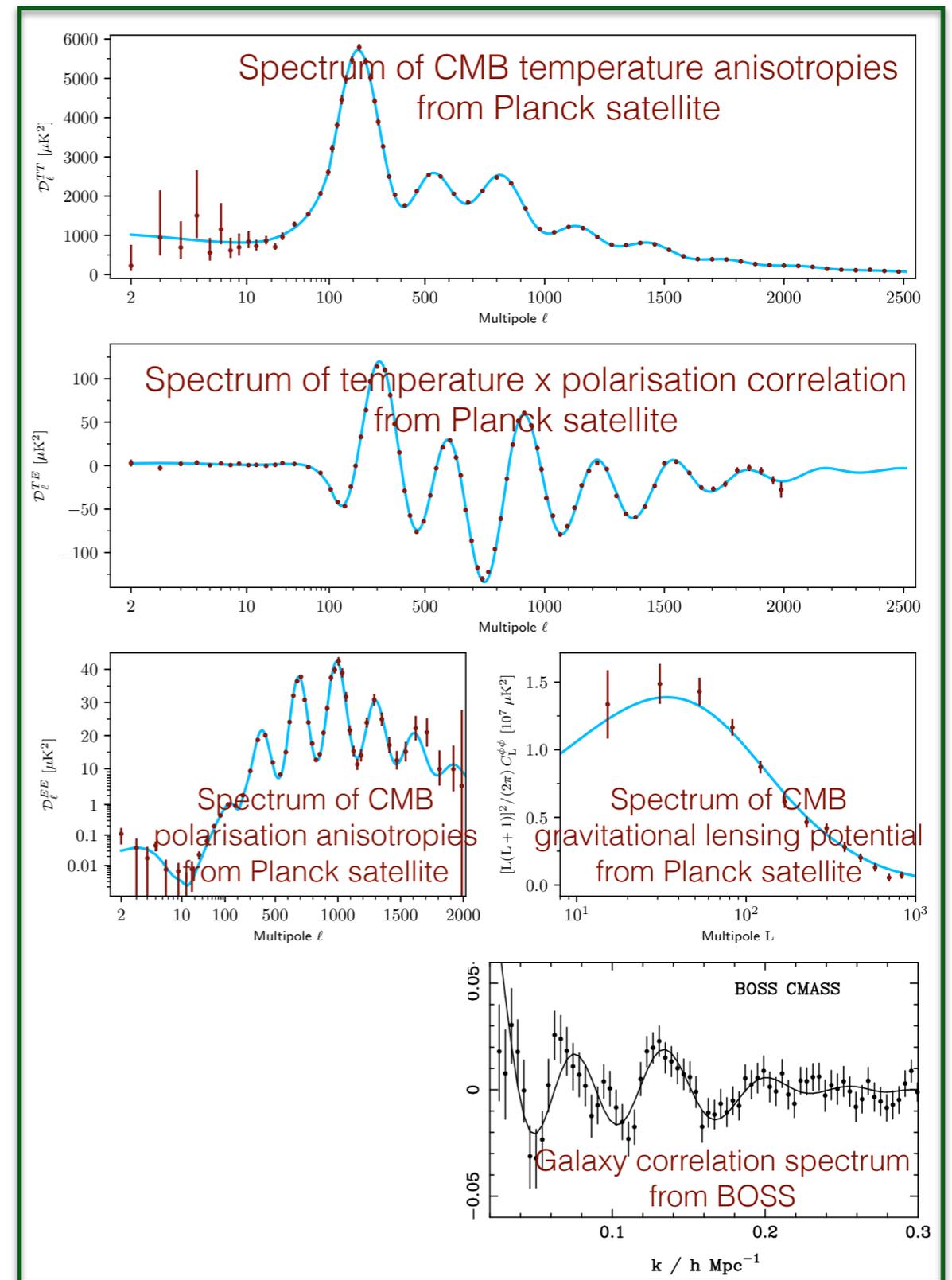
agreement of CMB and BAO with:

- CMB/BAO with BBN and primordial abundances,
- luminosity of distant SNIa,
- various probes of the Large Scale Structure...

CMB (+ BAO) probe directly:

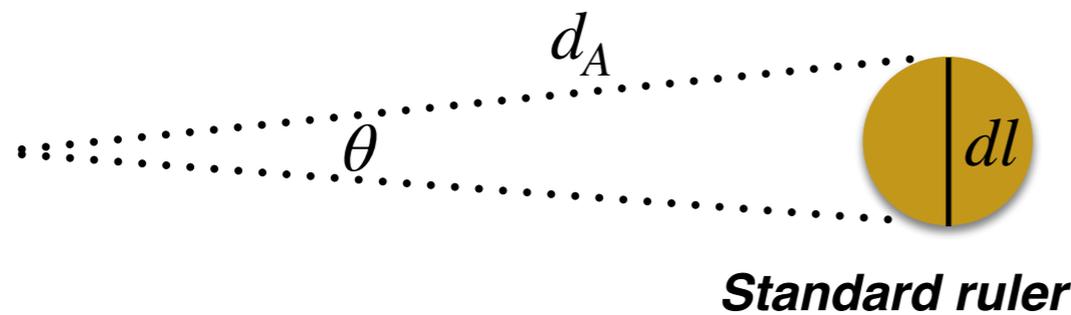
- $d_s \leftarrow$
- density ratio of baryon/photons,
 - density ratio of non-relativistic/relativistic matter,
- $\theta_s \leftarrow$
- angular scale of the sound horizon,
 - 2 params. for primordial spectrum,
 - optical depth to reionization

Indirectly: $\Rightarrow H_0 \equiv \frac{\dot{a}(t_0)}{a(t_0)} \sim 67 \text{ km/s/Mpc}$



Distances in cosmology

Angular diameter distance $d_A \equiv \frac{dl}{d\theta}$

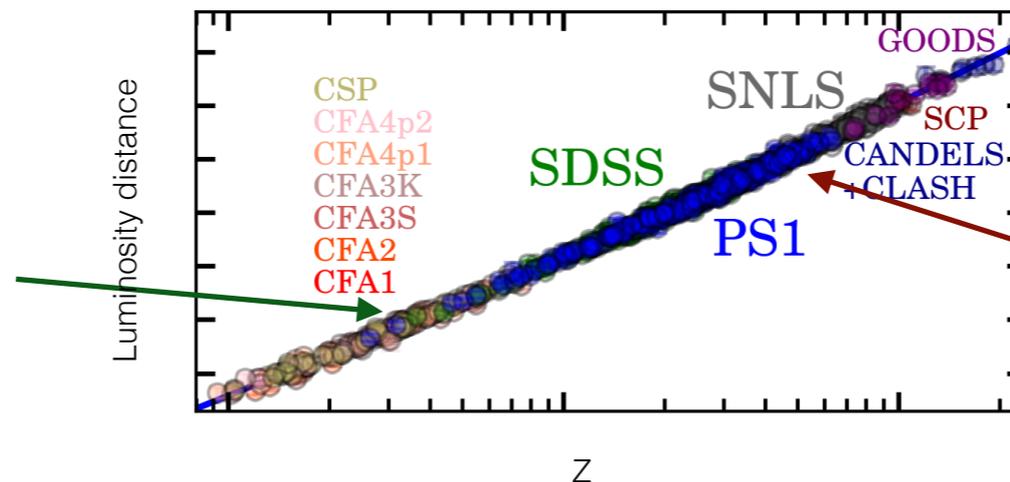


Luminosity distance $d_L \equiv \sqrt{\frac{L}{4\pi l}}$



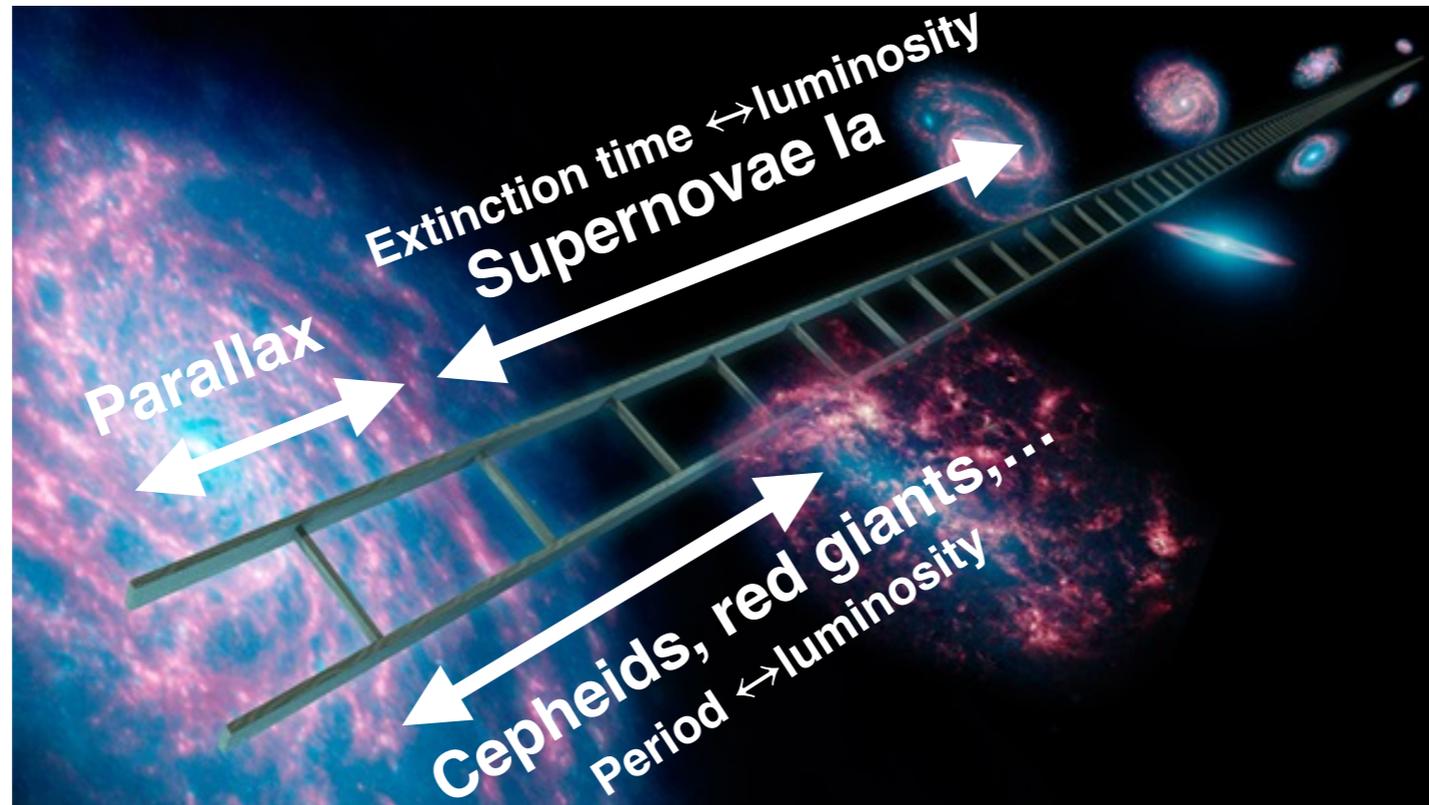
⇒ Measurement of H_0 by cepheids + SNIa: d_L vs. Redshift ! $d_L(z) = (1+z) \int_0^z \frac{d\tilde{z}}{H(\tilde{z})}$

nearby SNIa:
first derivative ⇒ H_0

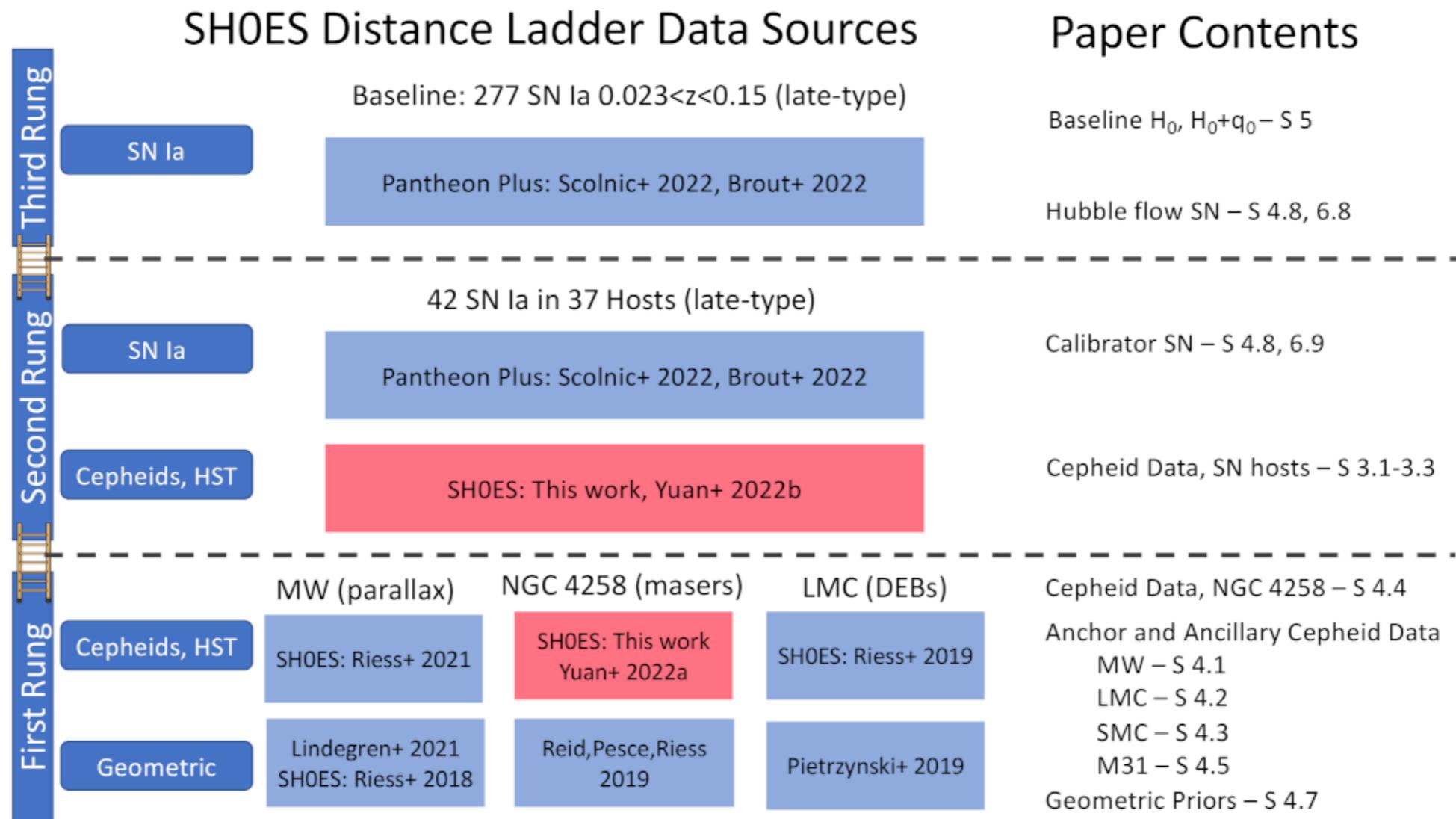


remote SNIa:
second derivative ⇒ Ω_k, Ω_Λ

Direct measurement of Hubble rate from standard candles

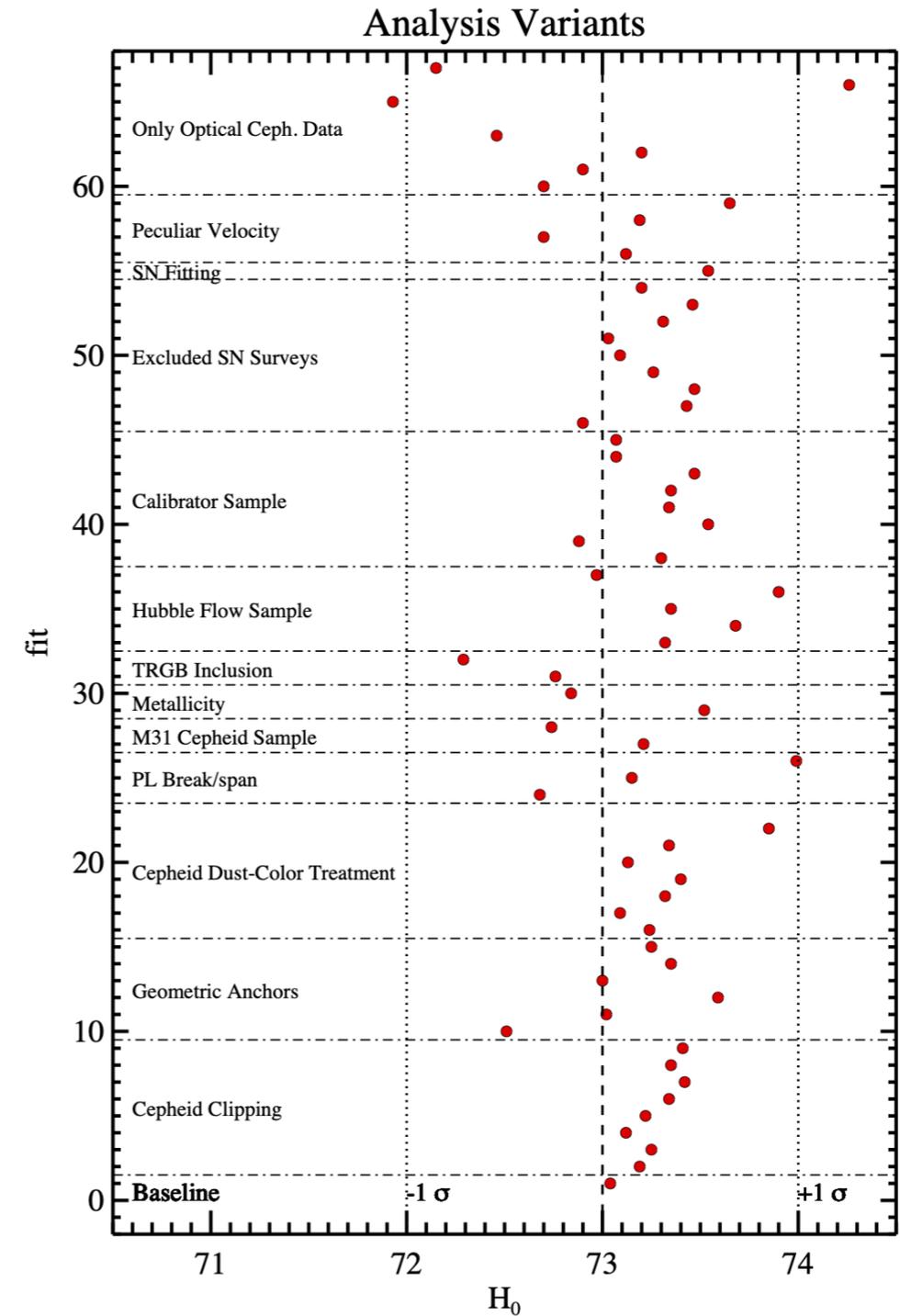


Direct measurement of Hubble rate from standard candles



Direct measurement of Hubble rate from standard candles

Systematics in direct H_0 measurements?
Environnement-bias of SNIa close to cepheids,
variations in cepheids:
Mortsell et al. 2105.11461, 2106.09400, ...



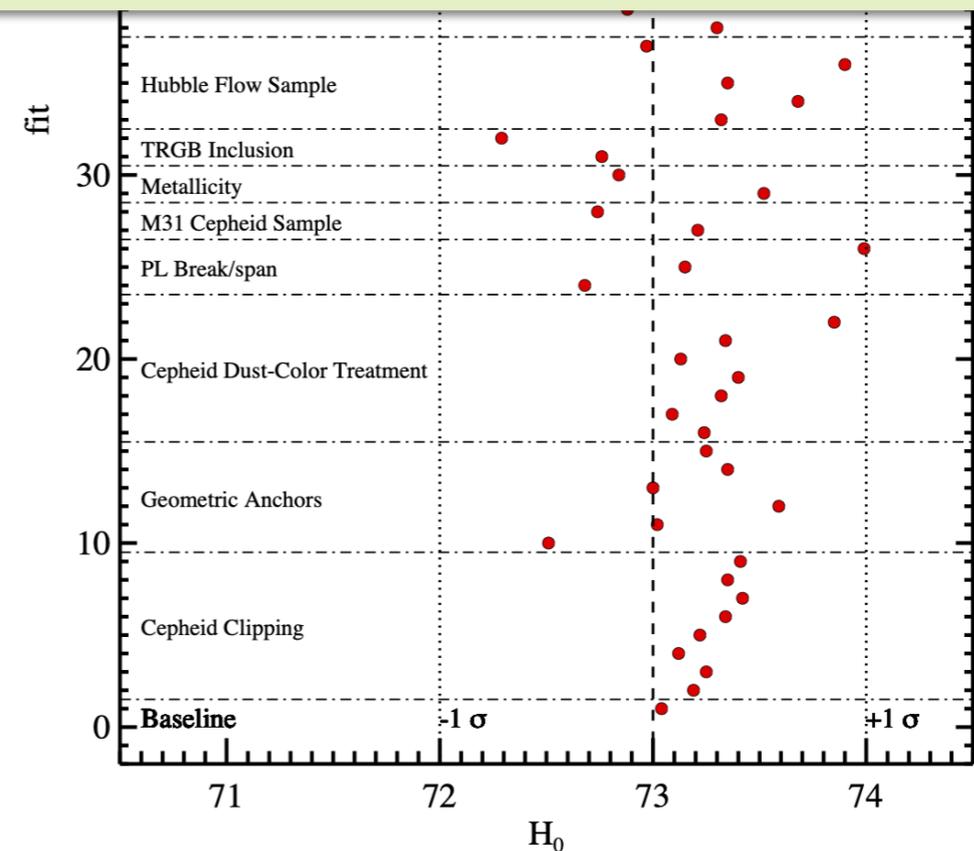
Riess et al. 22

Direct measurement of Hubble rate from standard candles

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Environnement-bias of SNIa close to cepheid
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Mortsell et al. 2105.11461, 2106.09400,....

How to settle the issue?

- Other standard candles:
 - Tip of Red Giant Branch (TRGB),
 - Black Holes as standard sirens (LISA, ET)
- Redshift drift (VLT, SKA)...



Riess et al. 22

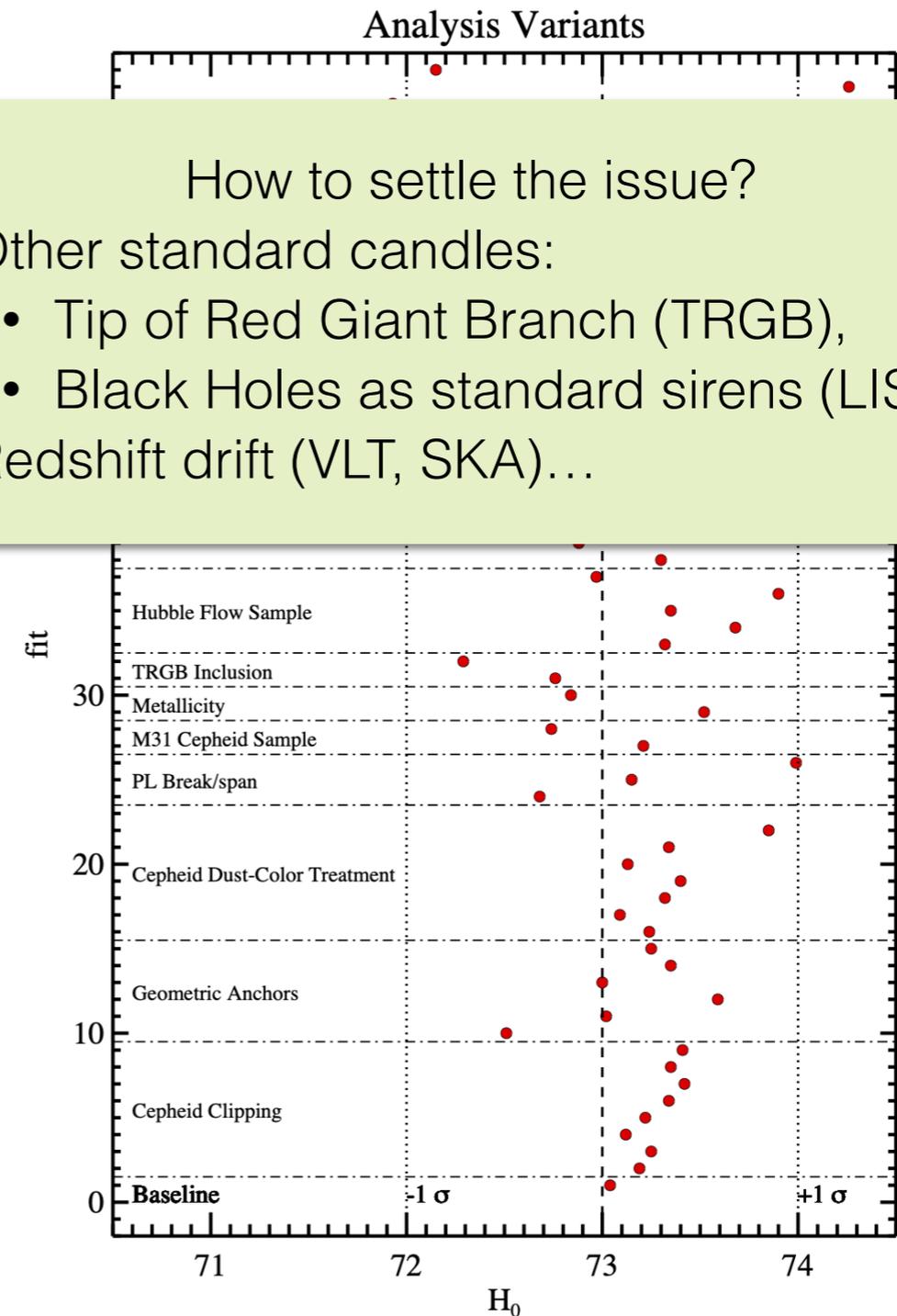
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- How to settle the issue?
- Other standard candles:
 - Tip of Red Giant Branch (TRGB),
 - Black Holes as standard sirens (LISA, ET)
 - Redshift drift (VLT, SKA)...

Systematics in CMB?
 Unknown foregrounds, insufficient instrument
 modelling...

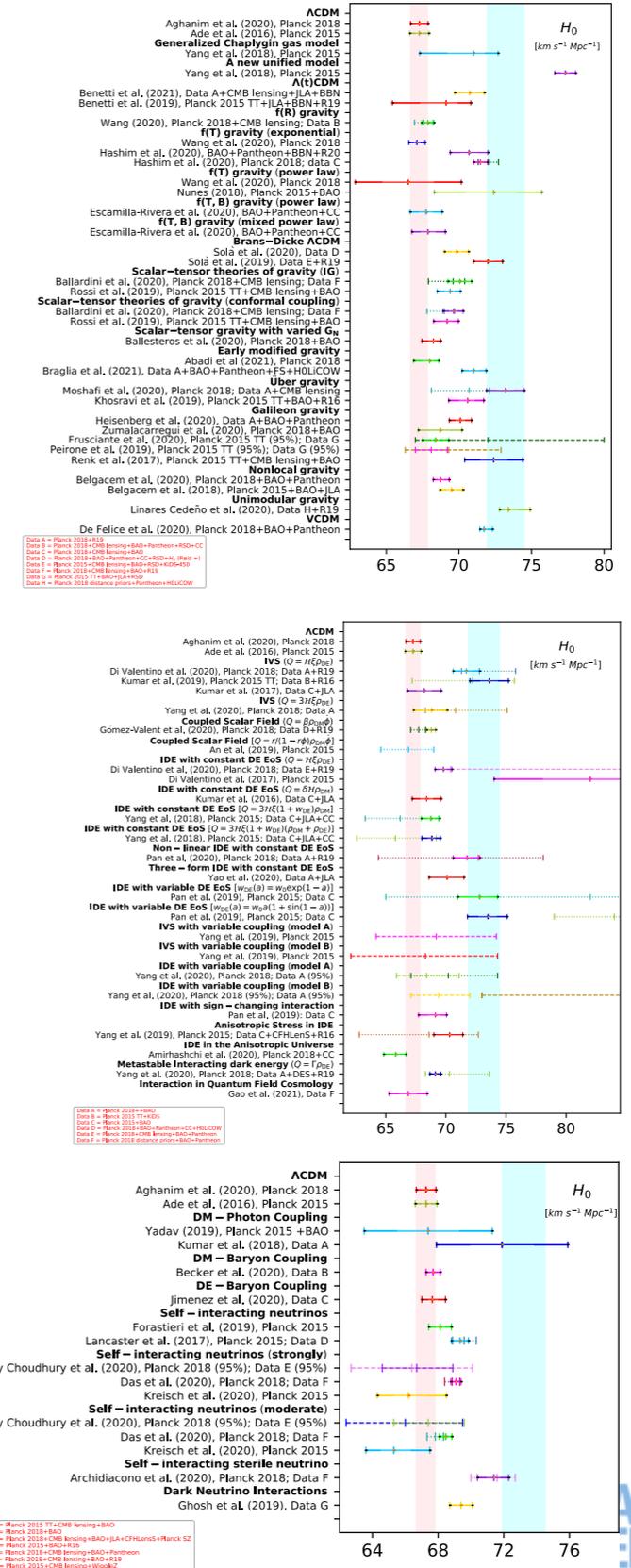
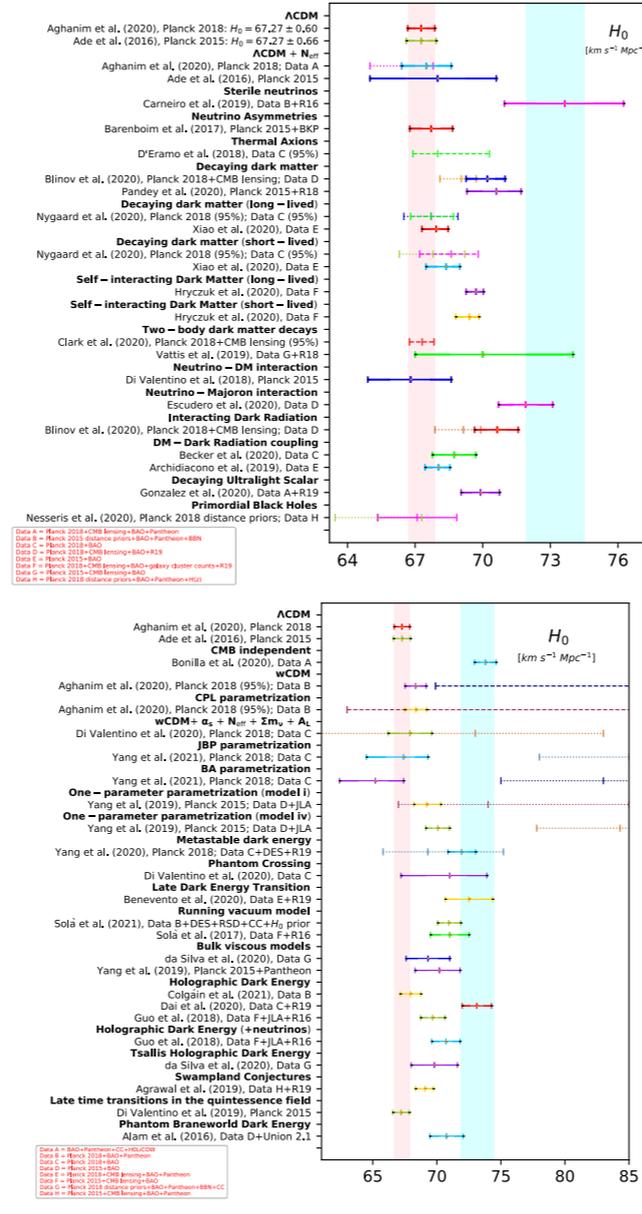
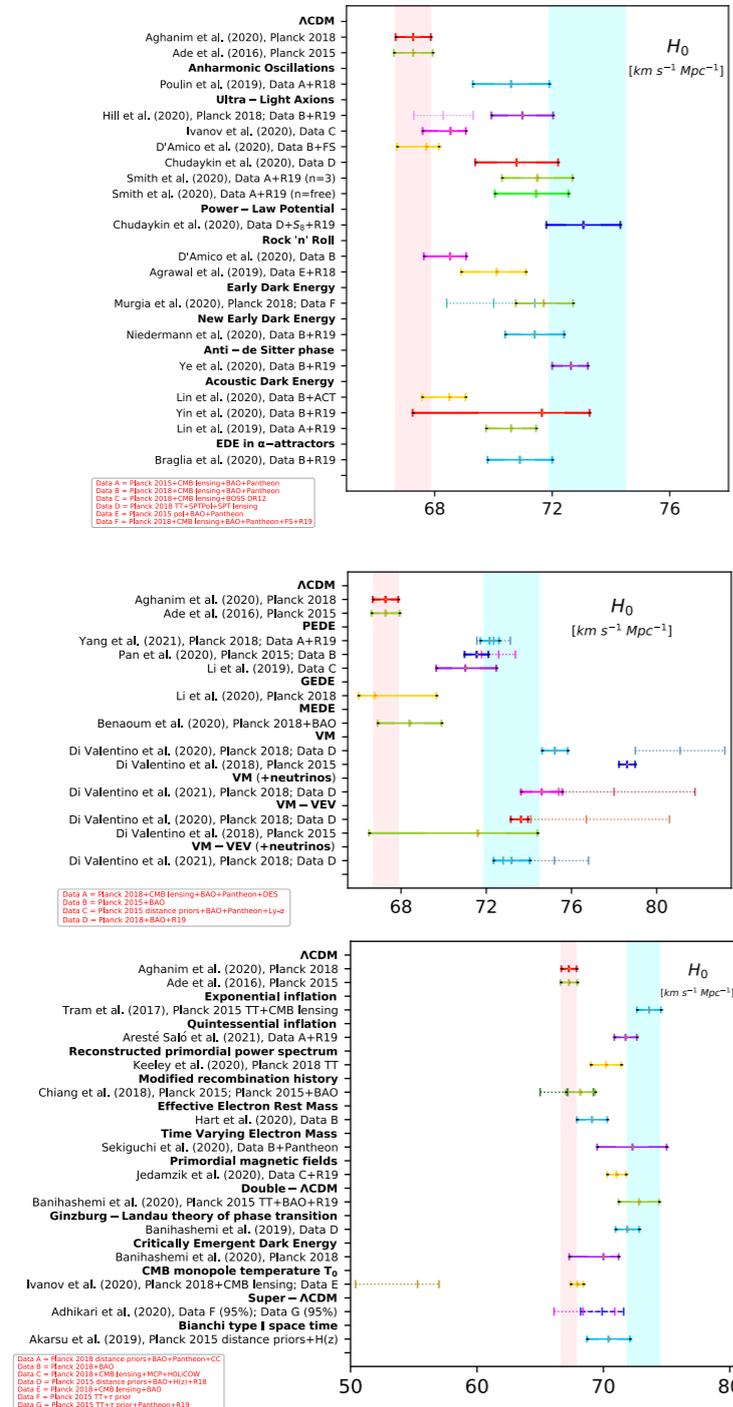
Small deviations from Λ CDM with new
 ingredients
 (DM, DE, MG, magnetic fields, etc.),
 or large-scale deviation from Friedmann model



Riess et al. 22

Solving the H_0 tension with extended cosmological models: exhaustive review

De Valentino et al. 2103.01183



Solving the H_0 tension with extended cosmological models: fair comparison

Schöneberg, Abellan, Pérez, JL, Witte, Poulin, Lesgourgues, 2107.10291, *Phys. Rep.* 984 (2022) 1-55

- Selection of 19 “representative models” (see later)
- Three metrics to quantify the (resolution of the) tension

Model	ΔN_{param}	M_B	Gaussian Tension	Q_{DMAP} Tension		$\Delta\chi^2$	ΔAIC		Finalist
ΛCDM	0	-19.416 ± 0.012	4.4σ	4.5σ	X	0.00	0.00	X	X
ΔN_{ur}	1	-19.395 ± 0.019	3.6σ	3.8σ	X	-6.10	-4.10	X	X
SIDR	1	-19.385 ± 0.024	3.2σ	3.3σ	X	-9.57	-7.57	✓	✓ ③
mixed DR	2	-19.413 ± 0.036	3.3σ	3.4σ	X	-8.83	-4.83	X	X
DR-DM	2	-19.388 ± 0.026	3.2σ	3.1σ	X	-8.92	-4.92	X	X
$\text{SI}\nu\text{+DR}$	3	$-19.440^{+0.037}_{-0.039}$	3.8σ	3.9σ	X	-4.98	1.02	X	X
Majoron	3	$-19.380^{+0.027}_{-0.021}$	3.0σ	2.9σ	✓	-15.49	-9.49	✓	✓ ②
primordial B	1	$-19.390^{+0.018}_{-0.024}$	3.5σ	3.5σ	X	-11.42	-9.42	✓	✓ ③
varying m_e	1	-19.391 ± 0.034	2.9σ	2.9σ	✓	-12.27	-10.27	✓	✓ ①
varying $m_e + \Omega_k$	2	-19.368 ± 0.048	2.0σ	1.9σ	✓	-17.26	-13.26	✓	✓ ①
EDE	3	$-19.390^{+0.016}_{-0.035}$	3.6σ	1.6σ	✓	-21.98	-15.98	✓	✓ ②
NEDE	3	$-19.380^{+0.023}_{-0.040}$	3.1σ	1.9σ	✓	-18.93	-12.93	✓	✓ ②
EMG	3	$-19.397^{+0.017}_{-0.023}$	3.7σ	2.3σ	✓	-18.56	-12.56	✓	✓ ②
CPL	2	-19.400 ± 0.020	3.7σ	4.1σ	X	-4.94	-0.94	X	X
PEDE	0	-19.349 ± 0.013	2.7σ	2.8σ	✓	2.24	2.24	X	X
GPEDE	1	-19.400 ± 0.022	3.6σ	4.6σ	X	-0.45	1.55	X	X
DM \rightarrow DR+WDM	2	-19.420 ± 0.012	4.5σ	4.5σ	X	-0.19	3.81	X	X
DM \rightarrow DR	2	-19.410 ± 0.011	4.3σ	4.5σ	X	-0.53	3.47	X	X

Table 1: Test of the models based on dataset $\mathcal{D}_{\text{baseline}}$ (Planck 2018 + BAO + Pantheon), using the direct measurement of M_b by SH0ES for the quantification of the tension (3rd column) or the computation of the AIC (5th column). Eight models pass at least one of these three tests at the 3σ level.

How to concile larger Hubble rate with observed θ_S ?

- **sound horizon angle** as seen by BAO or CMB must be preserved:

$$\theta(z) = \frac{\int_{z_D}^{\infty} c_s(\omega_b, \tilde{z}) H(\tilde{z})^{-1} d\tilde{z}}{\int_0^z H(\tilde{z})^{-1} d\tilde{z}}$$

redshift z = “look-back time”

Sound horizon =
integral over sound speed
from early universe till decoupling

Angular diameter distance =
integral over inverse Hubble rate
from observation till today

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- Global rescaling of $H(z)$?

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integral over inverse Hubble rate
from observation till today

- Global rescaling of $H(z)$?

Forbidden: at early time, related to density of photons, fixed by $T_{CMB} = 2.7255 \text{ K}$,
and to density of neutrinos, fixed by $N_\nu = 3$

Late time solutions

- **sound horizon angle** as seen by BAO or CMB:

$$\theta(z) = \frac{\int_{z_D}^{\infty} c_s(\omega_b, \tilde{z}) H(\tilde{z})^{-1} d\tilde{z}}{\int_0^z H(\tilde{z})^{-1} d\tilde{z}}$$

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integral over sound speed
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First idea: keep early cosmology unchanged; alter only *late* evolution $H(z)$ to get a large H_0 today
⇒ “Late time solutions”.

Late time solutions

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$$\theta(z) = \frac{\int_{z_D}^{\infty} c_s(\omega_b, \tilde{z}) H(\tilde{z})^{-1} d\tilde{z}}{\int_0^z H(\tilde{z})^{-1} d\tilde{z}}$$

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integral over inverse Hubble rate
from observation till today

First idea: keep early cosmology unchanged; alter only *late* evolution $H(z)$ to get a large H_0 today

⇒ “Late time solutions”.

Excluded by combination of BAO,
Supernovae, $H(z)$ data

“Shifted decoupling solutions”

- **sound horizon angle** as seen by BAO or CMB:

$$\theta(z) = \frac{\int_{z_D}^{\infty} c_s(\omega_b, \tilde{z}) H(\tilde{z})^{-1} d\tilde{z}}{\int_0^z H(\tilde{z})^{-1} d\tilde{z}} \stackrel{\Lambda\text{CDM}}{=} \frac{\int_{z_D(\omega_b, \Omega_m h^2)}^{\infty} \frac{c_s(\omega_b; \tilde{z}) d\tilde{z}}{\left[(1+\tilde{z})^3 + \frac{1.68\omega_\gamma}{\Omega_m h^2} (1+\tilde{z})^4 \right]^{1/2}}}{\int_0^z \frac{d\tilde{z}}{\left[\frac{1-\Omega_m}{\Omega_m} + (1+\tilde{z})^3 \right]^{1/2}}}$$

“Shifted decoupling solutions”

- **sound horizon angle** as seen by BAO or CMB:

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Second idea: preserve overall background evolution of ΛCDM , but anticipate the time of photon decoupling (*increase z_D*) and simultaneously of radiation-matter equality with larger h :

⇒ “Shifted decoupling” solutions

“Shifted decoupling solutions”

Issue: *recombination of protons + electrons* and *decoupling of photons* = accurately modelled processes; atom hydrogen model, fundamental constants (fine-structure constant, electron mass, Thomson scattering cross-section...) -> definite prediction for T_D and z_D

- First way: string theory / runaway-dilaton-inspired models with *running of the constants*: slightly different α or m_e at $z \sim 1000$ and $z \sim 1$ Hart & Chluba 2020
(e.g. $m_e \searrow$ by 0.5%: works very well) **golden medal**
- Second way: large inhomogeneities on very small scales (e.g. from primordial magnetic fields) -> *inhomogeneous recombination*, average recombination time decreased without changing the background model **bronze medal** Jedamzik & Pogosian 2020

Second idea: preserve overall background evolution of Λ CDM, but anticipate the time of photon decoupling (*increase z_D*) and compensate numerator with larger h :

⇒ “Shifted decoupling” solutions

“Early time solutions”

- **sound horizon angle** as seen by BAO or CMB:

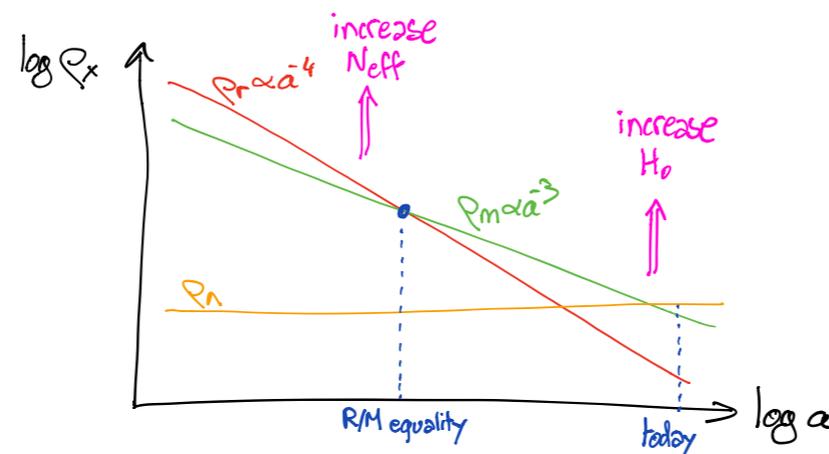
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Third idea: additional contribution to $H(z)$ in denominator (*enhanced radiation or something similar*) and compensate with larger h :
 \Rightarrow “Early time solutions”

“Early time solutions”

Third idea: rescale all densities equally and enhance $H(z)$ to get a large H_0 today

⇒ “Early time solutions”

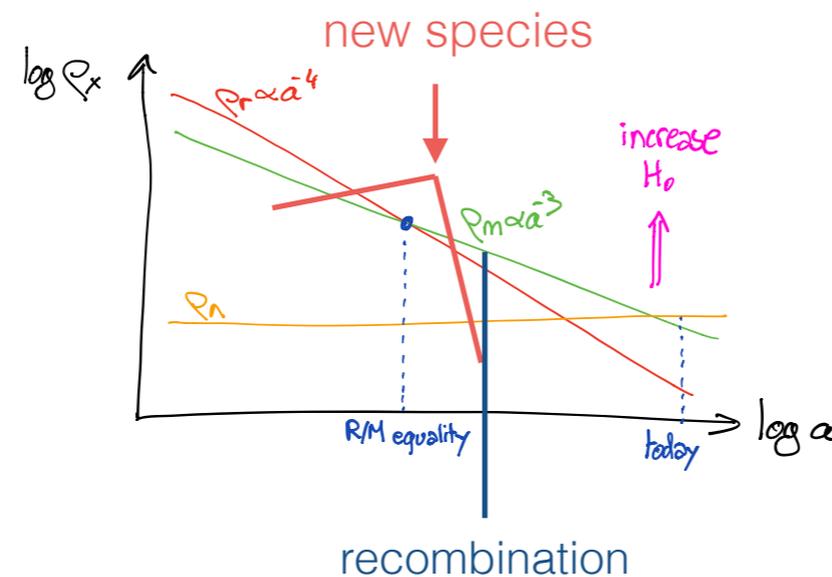


- Need to increase the relic density of relativistic species around the times relevant for the CMB: effectively, like “adding extra neutrino-like species” (effective neutrino number N_{eff}). Would need approximately 0.5 to 1 more...
- Issues:
 - incompatible with **Nucleosynthesis and primordial element abundances**: extra relics to be produced between “Nucleosynthesis times” and “CMB times”
 - Incompatible with **CMB spectrum shape** (scale of the peaks, enhanced Silk damping...) and **matter power spectrum amplitude/shape**, at least if extra relics are decoupled and free-streaming...
 - Baseline dataset: $N_{\text{eff}} = 3.1557 \pm 0.0677$ (68 % CL). Simple “ $\Lambda\text{CDM} + N_{\text{eff}}$ ” model fails!

“Early time solutions”

Third idea: rescale all densities equally and enhance $H(z)$ to get a large H_0 today

⇒ “Early time solutions”



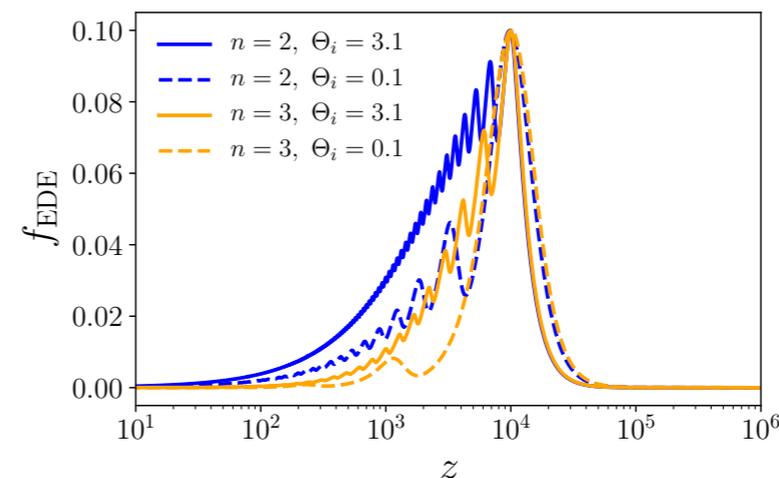
- Need to increase the expansion rate **only around recombination** with new particle, scalar field... escape **early BBN constraint** and **late Silk damping** constraint
- Possibly play with **other effects on perturbations** to cure CMB spectrum issues (additional ingredients to **increase DR clustering** before recombination and/or **decrease DM clustering** after recombination)

“Early time solutions”

1. use a **scalar field** to enhance $\rho_{\text{tot}}(z)$ and $H(z)$ for a short while around CMB decoupling time. Escapes Nucleosynthesis and CMB problems of Dark Radiation. **silver medal**

- Various **Early Dark Energy models** (= scalar field with a given potential) work well: **3 Silver medals** (and consistent with Nucleosynthesis bounds) [Kamionkowski et al.,...]

Enhancement of $\rho_{\text{tot}}(z)$ for various potentials \Rightarrow
(1st or 2nd order phase transition)



- Models are very *ad hoc*... attempts to connect it with particle physics: axion models, Xenon 1T anomaly (Poulin et al.) or sterile/active neutrino mass via inverse see-saw (Niedermann and Sloth)
- Exists in “modified gravity” version, e.g. with [Braglia et al. 2021]:

$$S = \int d^4x \sqrt{-g} \left[(M_{\text{pl}}^2 + \xi \sigma^2) \frac{R}{2} - \frac{g^{\mu\nu}}{2} \partial_\mu \sigma \partial_\nu \sigma - \Lambda \left(-\frac{\lambda \sigma^4}{4} \right) \right] + S_{\text{m}}.$$

- Still predictive models: future CMB polarisation observations

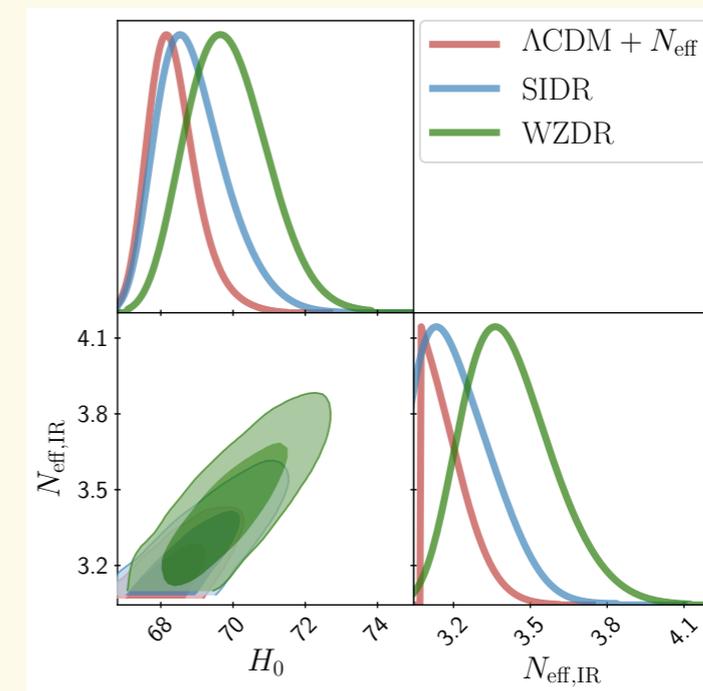
“Early time solutions”

Save $\Lambda\text{CDM}+N_{\text{eff}}$ with new physics in dark sector (non-standard interactions, decays, etc.)
changing the clustering properties and/or sound speed of Dark Radiation and/or Dark Matter...

2. self-interacting Dark Radiation to slow-down the particle velocity and change their clustering properties: **bronze medal** (provided that it gets populated after Nucleosynthesis).

Aloni, Berlin, Joseph, Schmaltz & Weiner 2111.00014; Schöneberg & Abellan 2206.11276
transform this into a **silver medal**; similarities with previous “sterile neutrinos with secret interactions” of Archidiacono, Hannestad et al.

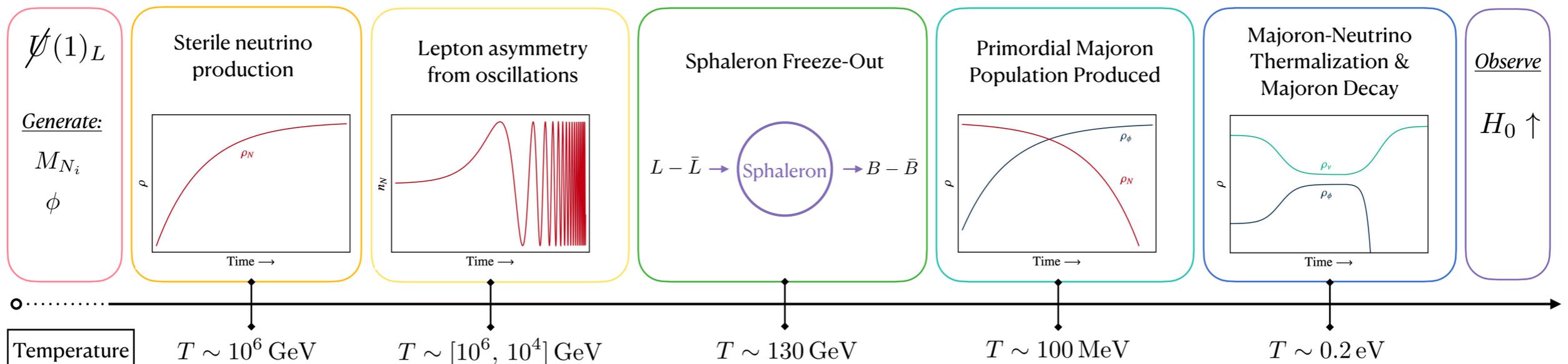
- Wess-Zumino Dark Radiation (WZDR) model of 2111.00014 :
 - Interaction between massless relic fermions (DM and DR) mediated by **eV-mass scalar** ($eV \sim M_{\text{SUSY}}^2/M_{\text{Pl}}$)
 - At $T \sim 1\text{eV}$, scalar becomes non-relativistic, entropy release boosts N_{eff} from ~ 3.3 to ~ 3.5 (precise value depends on T_{dark})
 - Transition leaves imprint in CMB spectrum that compensates for increase of (N_{eff}, H_0)



“Early time solutions”

3. particular realisation of a Majoron scenario of Escudero & Witte 1909.04044, 2004.01470, 2103.03249: **Silver medal** (and consistent with BBN bound)

- O(eV)-mass Majoron ϕ = pseudo-Goldstone of spontaneously broken $U(1)_L$
- small Yukawa-like couplings to active neutrinos
- $T \sim m_\phi$: interactions between majoron and active neutrinos (inverse neutrino decay):
 - Majoron thermalize and contribute to N_{eff} ,
 - active neutrinos do not free-stream
- $T \sim m_\phi/3$: Majoron decays into active neutrinos, which free-stream



Conclusions

- In terms of model-building, need to pay a high price, but reassuring that **we cannot fit anything...**
- Hope that one or more tension **solved by systematics!** Will know with better data and also new techniques: **Tip of the Red Giants Branch (TRGB)**, **redshift drifts (SKA, ELT)**, **GWs as standard sirens (LISA, ET...)**

If tension do not arise from systematics:

- Previous models: predictions for **next-generation CMB/LSS: SO, CMB S4, Euclid, Rubin...** (e.g. EDE, Majoron, shifted recombination...)
- Chance to learn about **new particle physics**, tests it in laboratory? (e.g. DM interactions, Majoron)
- Revisit models **beyond Friedmann?** Large-scale inhomogeneity?

Introductory material

Solving the H_0 tension with extended cosmological models: fair comparison

Schöneberg, Abellan, Pérez, JL, Witte, Poulin, Lesgourgues, 2107.10291

- Selection of 19 “representative models” (see later)
- Data sets:
 - **Baseline:** *Planck 2018 (incl. lensing) + BAO + Pantheon + SH0ES* treated as measurement of intrinsic magnitude M_B
 - **Additional tests** with *Planck* -> *BAO+BBN* or *WMAP+ACT*, and with *RSD, CC, BAO-Lya*
- **Three metrics** to quantify the (resolution of the) tension:
 1. *When considering a data set D that does not include SH0ES, what is the residual level of tension between the posterior on M_B inferred using D and the SH0ES measurement?*

$$\frac{\bar{x}_D - \bar{x}_{\text{SH0ES}}}{(\sigma_D^2 + \sigma_{\text{SH0ES}}^2)^{1/2}} \quad \text{where } x \equiv M_B$$

2. *How does the addition of the SH0ES measurement to the data set D impact the fit within a particular model M ?*

$$\Delta\chi^2 = \chi_{\min, D+\text{SH0ES}}^2 - \chi_{\min, D}^2 - \chi_{\min, \text{SH0ES}}^2$$

3. *When the data set D includes the SH0ES data on M_B , does the fit within a particular model M significantly improve upon that of ΛCDM ?*

$$\Delta\text{AIC} = \chi_{\min, \mathcal{M}}^2 - \chi_{\min, \Lambda\text{CDM}}^2 + 2(N_{\mathcal{M}} - N_{\Lambda\text{CDM}})$$

Solving the H_0 tension with extended cosmological models: fair comparison

Schöneberg, Abellan, Pérez, JL, Witte, Poulin, Lesgourgues, 2107.10291

Planck 2018 (incl. lensing) + BAO + Pantheon + SH0ES

